



Copy number variation detection with whole genome sequencing data

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Copy number variation (CNV)

- CNVs: gains or losses of genomic segments
- CNVs accounts for a substantial proportion of human genomic variations
 - In the Database of Genomic Variation (DGV), over 30% of human genome can be influenced by CNVs
- CNVs have been associated with a wide spectrum of diseases
 - Autism, Schizophrenia and Obesity
- In Cancer genomes, we often see very large copy gains of losses

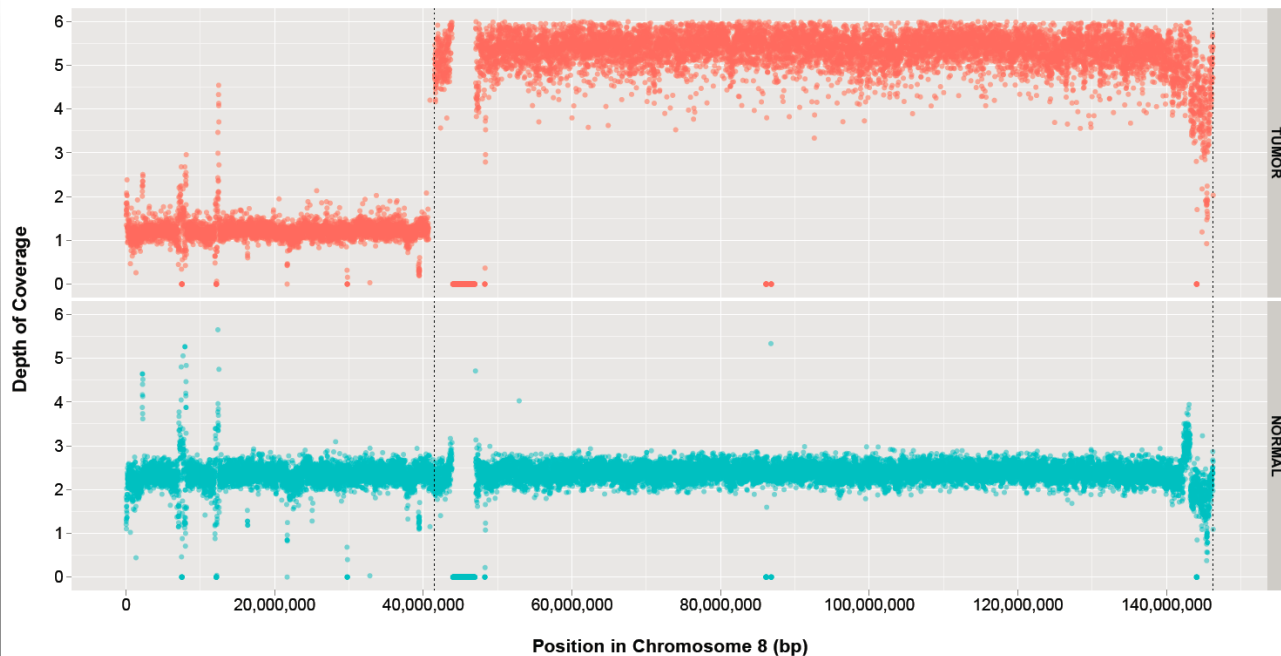
Next-generation sequencing (NGS)



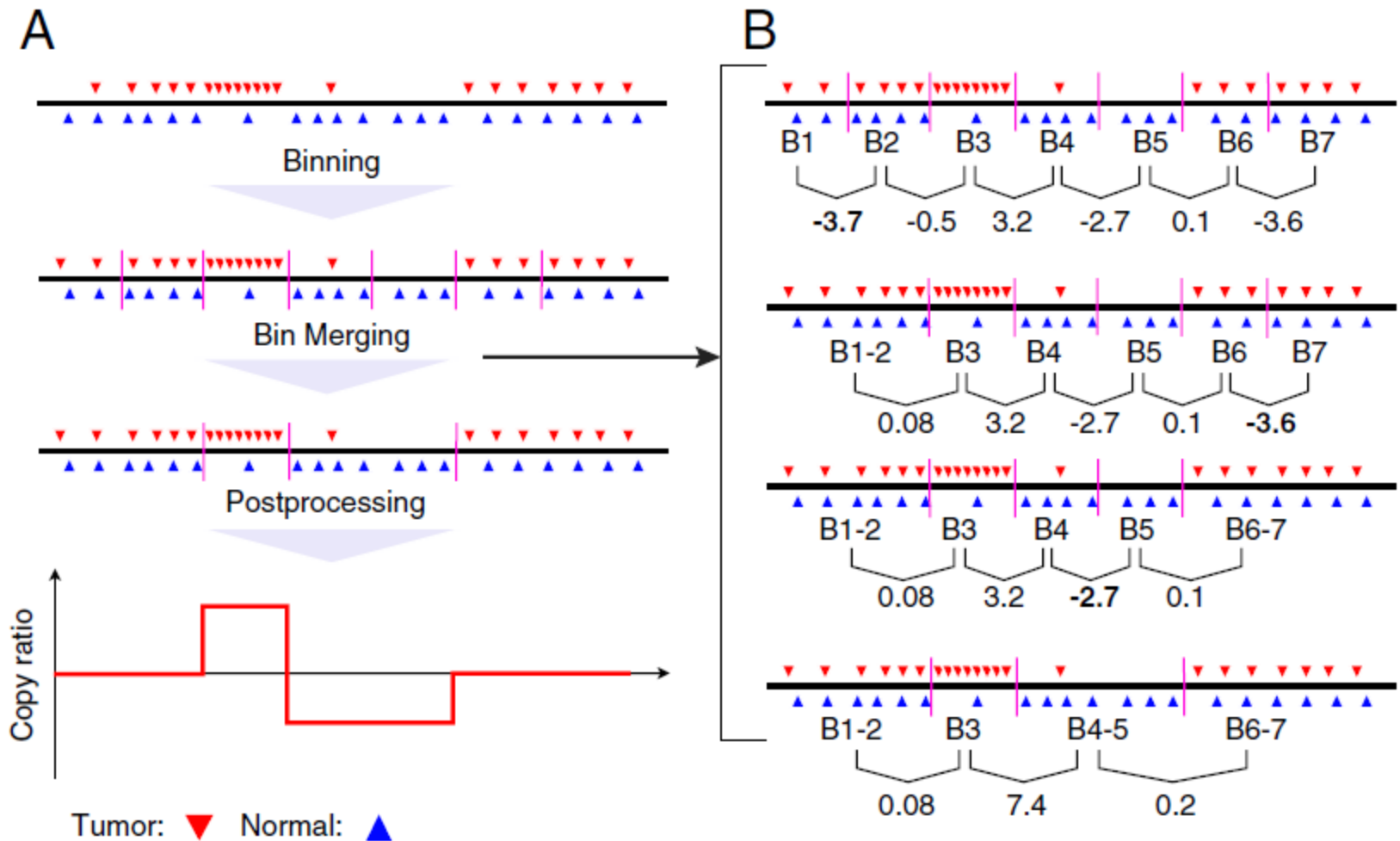
- NGS platforms
 - Roche 454 platforms
 - Illumina/Solexa platforms (most widely used)
 - Applied Biosystem (ABI) SOLiD
 - Helicos HeliSope™ sequencer(single molecular sequencing)
 - Life Technologies platforms
- The throughput is increasing and the price is dropping
- Short read but high throughput

CNV detection using read-depth

- Read-depth: read density in a genomic region
- If there is no bias, the read-depth in a genomic region should be roughly proportional to the copy number
- But there are often biases in the NGS data.



BIC-seq: an algorithm for detecting somatic CNVs in tumor genomes



Statistical Model

- Given a short read R that is mapped to the reference genome, it consists of two pieces of information
 - The position s on the reference genome
 - The read type Y : tumor ($Y=1$) or normal ($Y=0$).
- Assume the distribution of $R=(Y, S)$ is $f(y, s)$.
- By Bayes' theorem

$$\begin{aligned} f(y, s) &= \Pr(Y = y \mid S = s) \Pr(S = s) \\ &= \Pr(Y = y \mid S = s) f(s), \end{aligned}$$

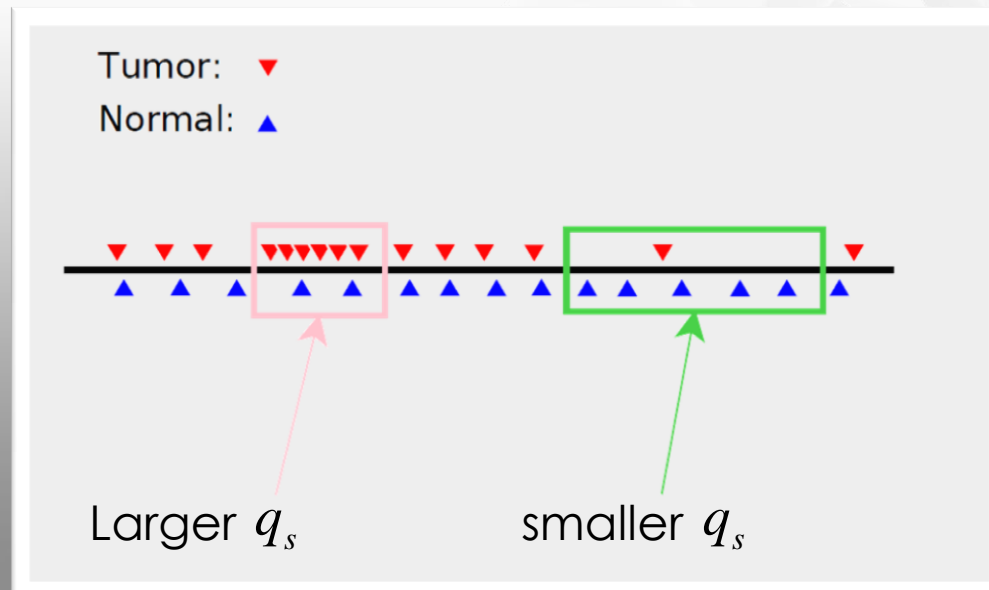
where $f(s)$ is the marginal distribution of S .

Statistical Model (cont. 1)

- Denote q_s be the probability of a read at position s being a tumor read, i.e. $q_s = \Pr(Y = 1 | S = s)$.
- Given N mapped short reads $R_1 = (y_1, s_1), \dots, R_N = (y_N, s_N)$, the joint likelihood is

$$L_N = \prod_{i=1}^N q_{s_i}^{y_i} (1 - q_{s_i})^{1-y_i} f(s_i)$$

- To identify CNV regions, it is enough to identify the breakpoints.



Statistical Model (cont. 2)

- Assume that q_s is a constant between any two neighboring breakpoints.
- Given the breakpoints $0 = \tau_0 < \tau_1 < \dots < \tau_m < \tau_{m+1} = L_c$ on a chromosome c , where L_c is the length of the chromosome c .
- Let p_j be the common probabilities q_s between the breakpoints τ_j and τ_{j+1} . The likelihood can be written as

$$L_N = \prod_{j=0}^m \prod_{\tau_j < s_i \leq \tau_{j+1}} p_j^{y_i} (1 - p_j)^{1-y_i} f(s_i),$$

- One set of breakpoints corresponds to one model. Then, we could use a model selection criterion such as the Bayesian information criterion (BIC) to select the breakpoints.

Bayesian information criterion (BIC)

- The general definition of the BIC of a model is

$$\text{BIC} = -2\log(L) + k\log(n),$$

- L : the likelihood function evaluated at the MLE
- k : the number of parameters in the model
- n : the total number of observations

BIC (cont.)

➤ Given the breakpoints $0 = \tau_0 < \tau_1 < \dots < \tau_m < \tau_{m+1} = L_c$, the BIC is

$$\begin{aligned} \text{BIC}(\lambda) = & -2 \sum_{j=0}^m [k_j \log(\hat{p}_j) + (n_j - k_j) \log(1 - \hat{p}_j)] \\ & -2 \sum_{i=1}^N f(s_i) + (m+1)\lambda \log(N), \end{aligned}$$

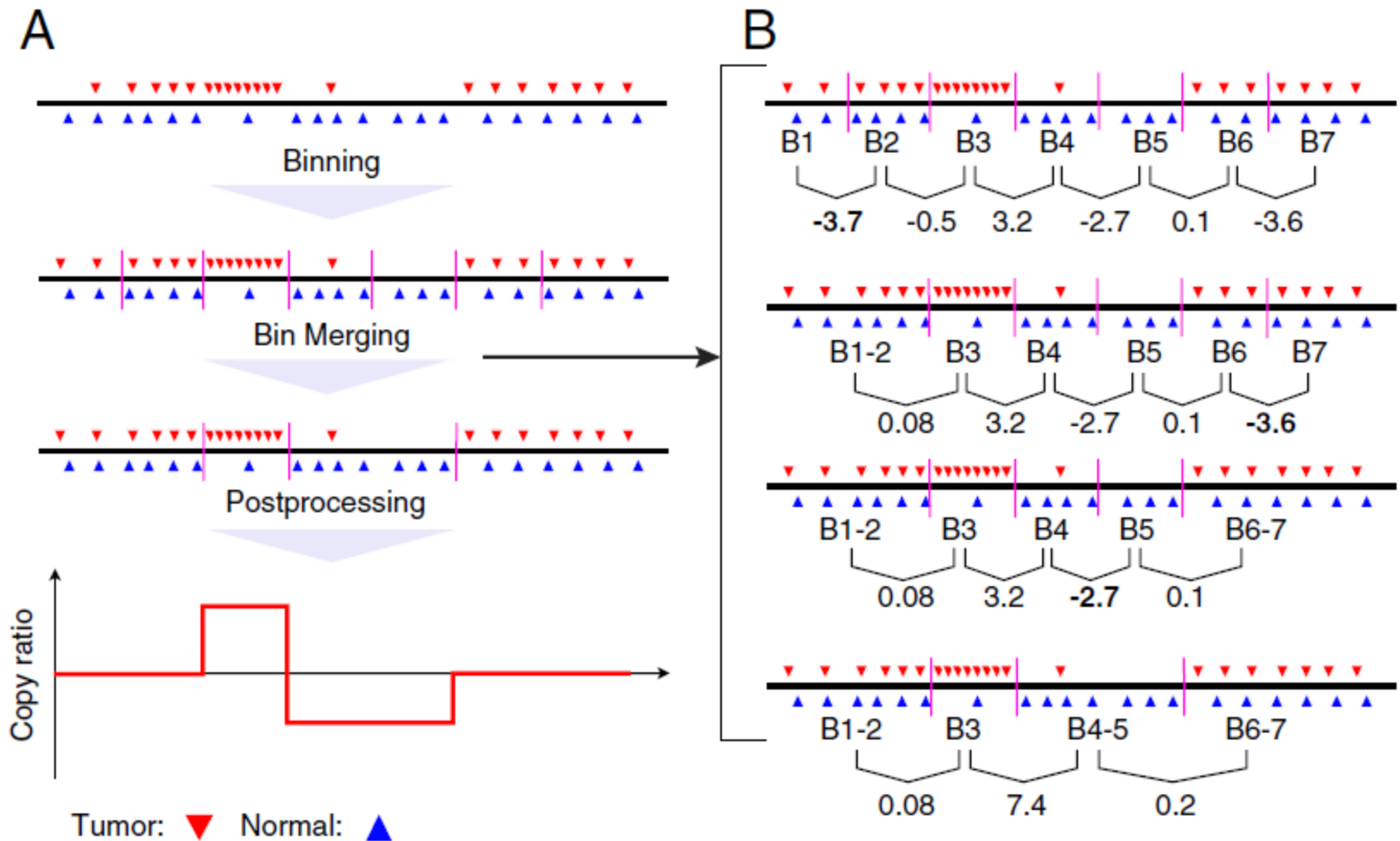
- k_j : the number of tumor reads between τ_j and τ_{j+1} .
- n_j : the total number of reads between τ_j and τ_{j+1}
- $\hat{p}_j = k_j / n_j$: the MLE of the parameter p_j
- $\lambda > 0$: tuning parameter

➤ Note that the term $-2 \sum_{i=1}^N f(s_i)$ is common for all different models. Therefore, we can drop it when comparing different models.

Asymptotic result

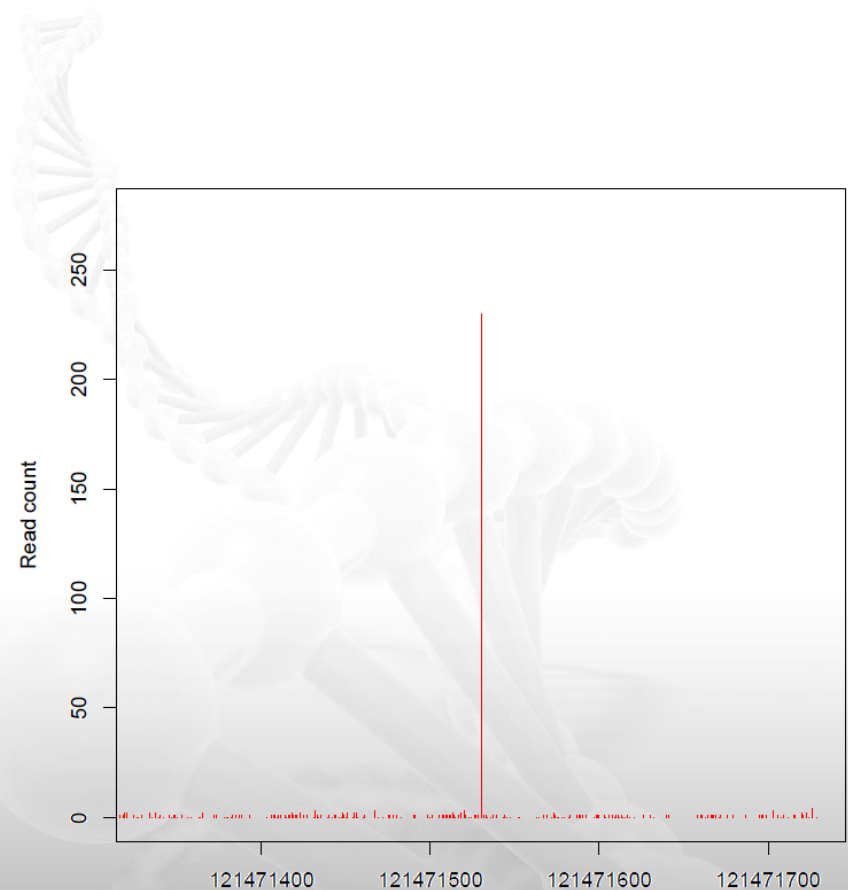
- Assume $f(s) > 0$ for all s . Then, the breakpoint set that minimizes the BIC is a consistent estimator of the true breakpoint set, i.e. it will converge to the true breakpoint set in probability as N , the number of observations, goes to infinity.

The BIC-seq algorithm (revisit)



Some remarks

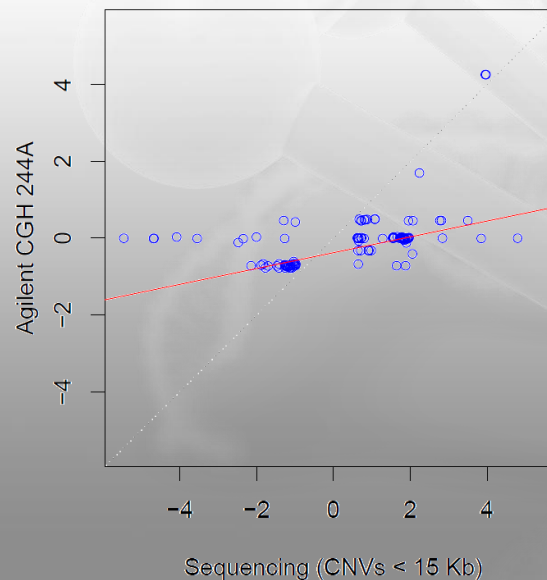
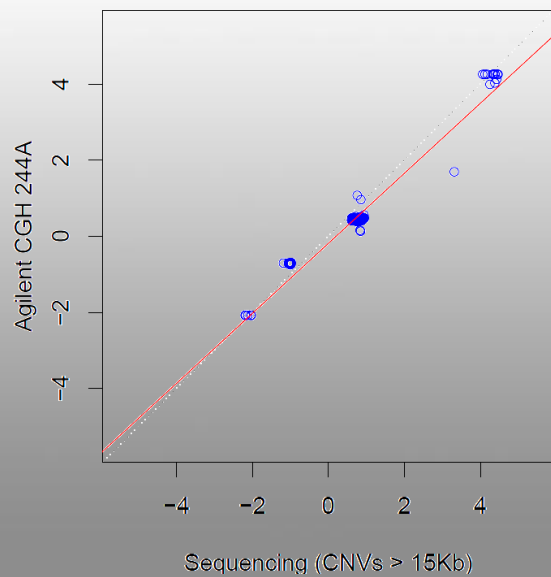
- Outlier removal:
 - Look at local genomic window to determine if the read count at a nucleotide position is an outlier
- Assign credible interval to a breakpoint
 - Gibbs sampling
- Assign false discovery rate
 - Permutation based



An outlier example

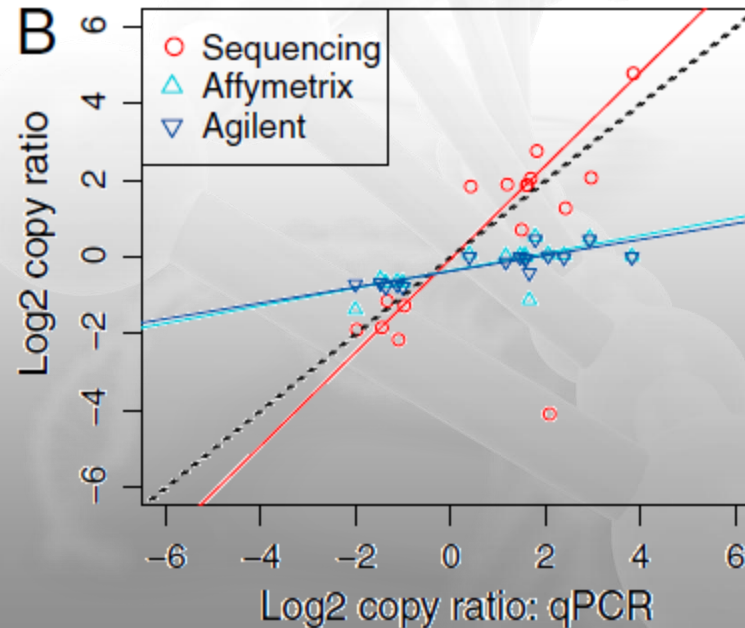
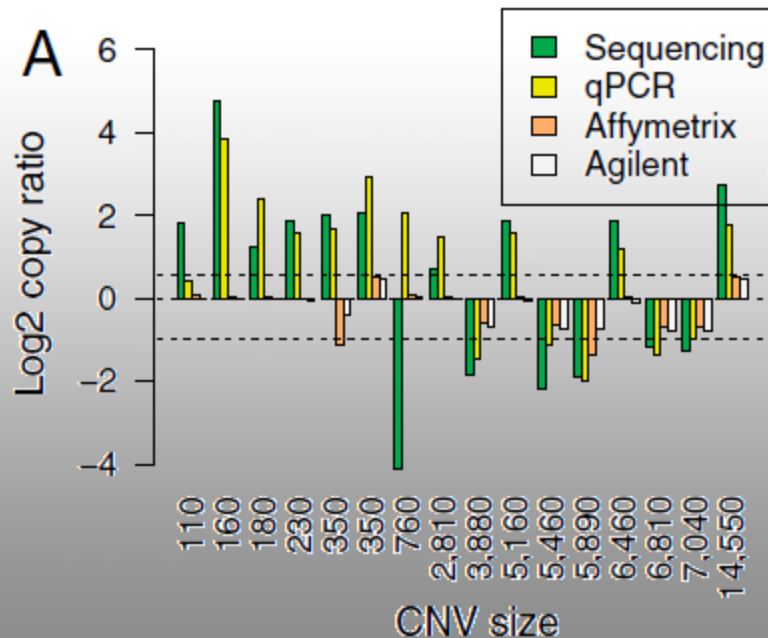
Application of BIC-seq on a GBM tumor genome

- Applied BIC-seq on a GBM tumor genome
 - Tumor: 10X
 - Normal: 7x
- Detected 291 putative CNVs ranging from 40bp to 5.7 Mb
- Compare the copy ratio estimate given by BIC-seq and an array-based platform



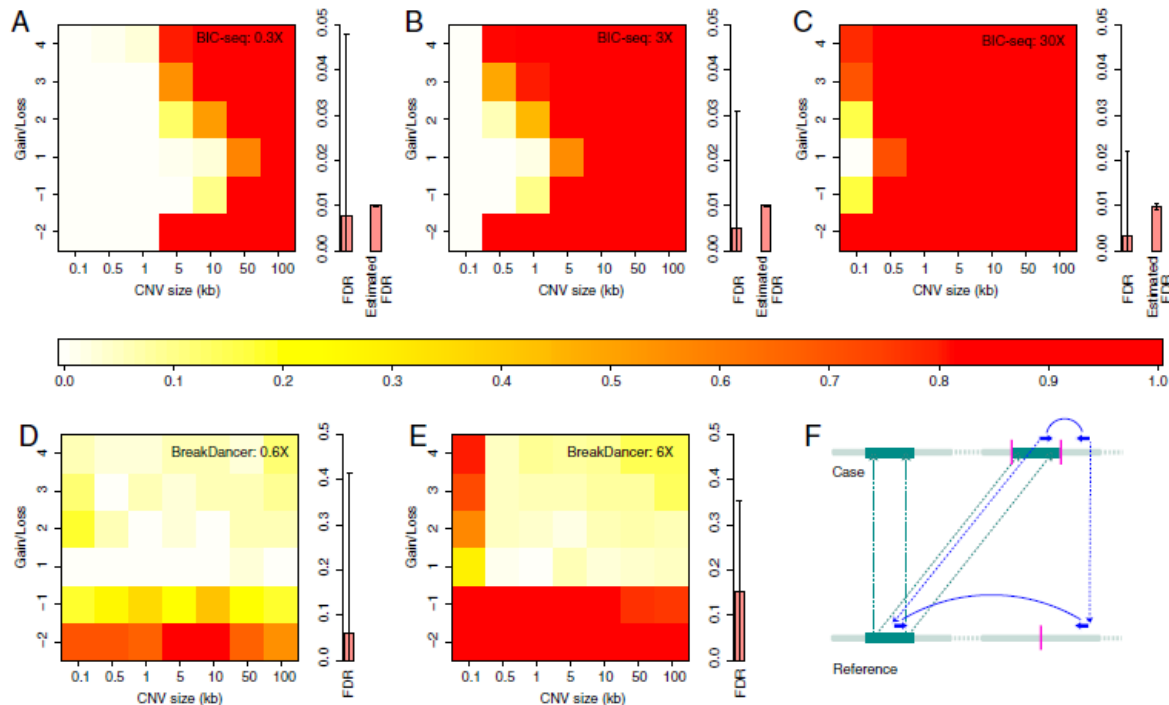
Application of BIC-seq on a GBM tumor genome (Cont.)

- Selected 16 small CNVs ranging from 110 bp to 14 kb for qPCR validation
- 14 out of 16 (87.5%) were validated



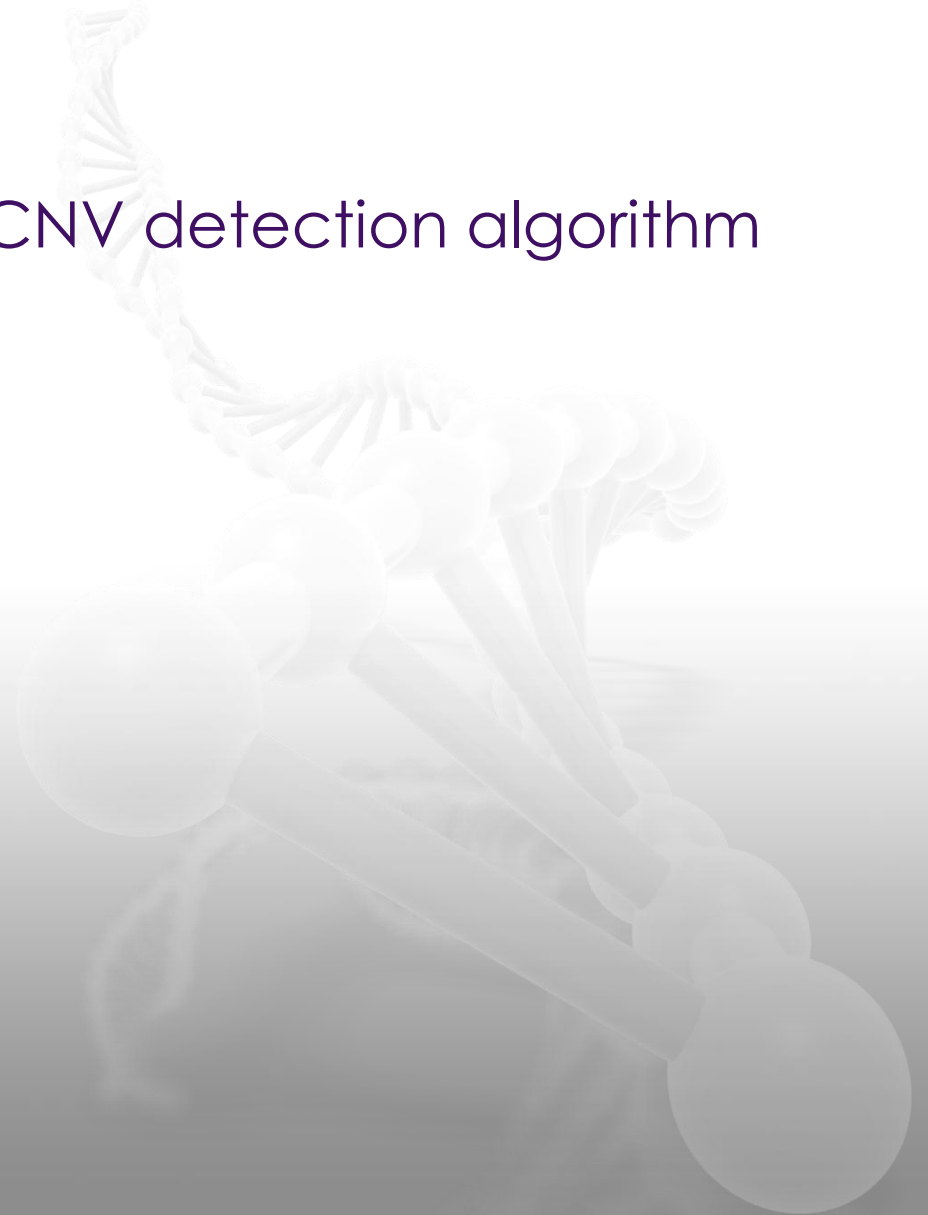
Comparison with a PEM method BreakDancer

- Use simulation for comparison
- Created 100 “tumor” chromosomes using chromosome 22 (hg18) as the template
 - Each tumor chromosome contains 42 CNV regions
 - 7 sizes and 6 copy numbers



Summary

- BIC-seq : a read-depth CNV detection algorithm
 - Nonparametric
 - Computationally efficient
 - High accuracy
 - Asymptotically consistent
 - High validation rate



A faint, stylized illustration of a DNA double helix and a molecular structure, possibly a protein or enzyme, rendered in a light gray color. The DNA helix is positioned in the upper right, and the molecular structure is more complex, with various spheres and connecting lines, located in the lower right. The background is a light gray gradient.

Thank you for your attention!