

概率论系列报告

报告题目 (Title) : From infinite urn schemes to decompositions of self-similar Gaussian processes

报告人 (Speaker) : 王一早 博士 University of Cincinnati

时间 (Time) : 6月6日(周一)下午 3:00-4:00

地点 (Venue) : 北京大学理科一号楼 1303

摘要 (Abstract) : We investigate a special case of infinite urn schemes first considered by Karlin (1967), and especially its occupancy and odd-occupancy processes. We first propose a natural randomization of these two processes and their decompositions. We then establish functional central limit theorems, showing that each randomized process and its components converge jointly to a decomposition of certain self-similar Gaussian process. In particular, the randomized occupancy process and its components converge jointly to the decomposition of a time-changed Brownian motion $\mathbb{B}(t^\alpha)$, $\alpha \in (0,1)$, and the randomized odd-occupancy process and its components converge jointly to a decomposition of fractional Brownian motion with Hurst index $H \in (0,1/2)$. The decomposition in the latter case is a special case of the decompositions of bi-fractional Brownian motions recently investigated by Lei and Nualart (2009). The randomized odd-occupancy process can also be viewed as a correlated random walk that scales to a fractional Brownian motion.

Joint work with Olivier Durieu (Université de Tours, France).

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