Atelier B

Reusable Components

Reference Manual

version 3.6



ATELIER B Reusable Components—Reference Manual version 3.6

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Introduction

The reusable components supplied with Atelier B are basic machines and library machines.

Basic machines are the modelisation in B of modules manually coded in C, C++ or ADA. These modules are used to encapsulate the operating system functions that must be used; they must usually be performed in taking into account the specificities of the hardware that the security software will run on. This is why there are few basic machines delivered with "Atelier B".

Library machines are abstract machines written in B language. They generally model a type of mathematical object (sequence, function, etc.) and offer the operations that allow the handling of these objects.

Unlike basic machines, library machines are properly performed using the B method, i.e, using refining and implementation in B along with complete proof of the set. This proof may in principle be executed at any time in order to check its validity (warning: proving methods may depend on the demonstrator version used). Therefore, unlike basic machines, library machines may be numerous and complex while remaining secure as they are proven.

To use basic machines, simply reference them in the appropriate B project, by INCLUDES, IMPORTS or any derived actions. When the final project is translated into a traditional programming language, the translation of the library machine implementations used must be redone if this was not already done at Atelier B installation.

Library machines are implemented on basic machines. As they are performed until the implementation in B language, they provide complete examples of use in the B method. They especially contain examples of proven WHILE loops. For practical advice on proving WHILE loops, refer to the "B Language User Manual".

The user may directly use library machines just like he uses basic machines. Sometimes the implementation of a library machine may use the services of a machine that it does not create an instance for (use by SEES) to avoid duplications. In this case the user will have to create the instance in question (using IMPORTS) by following the indications in the "IMPORTS REQUIRED" section of the description for each library machine.

When the final project C, C++ or ADA compilation is performed, the library compilation is automatically performed if necessary. Performing link editing will then enable incorporation into the final executable program only those object files that correspond to the library machines actually used. All this is performed in the *Makefile* produced by Atelier B. To integrate a software component produced by Atelier B into a traditional product, use this *Makefile* as a basis or refer to the "ADA Translator User Manual".

Warning:

This warning regards the use of reusable components with the Ada, C and C++ translators

supplied with Atelier B. These translators are experimentals. Their goal is to show that it is possible to translate some B0 implementations into classical programming languages. Therefore, their use is not guaranteed. Especially the reusable components use may induce errors when compiling the code produced by the translators. The reusable components must be considered as examples. Each user can develop his own library machines according to his needs. 2

Index of Basic Machines

BASIC_ARRAY_VAR: implanting a one dimension table

VAL_ARRAY read a table element

STR_ARRAY write a table element

BASIC_ARRAY_RGE: implementing a two dimensional table

VAL_ARR_RGE $\;$ read a table element

 STR_ARR_RGE write a table element

COP_ARR_RGE $% \left({{\rm{COP}}_{\rm{ARR}}} \right)$ copy a table line to another

CMP_ARR_RGE compare two table lines

BASIC_IO: vt 100 style input/output

INTERVAL_READ entry by the operator of a number in mm..nn.

INT_WRITE print a number.

BOOL_READ entry by a TRUE or FALSE boolean operator

BOOL_WRITE print the TRUE or FALSE condition.

CHAR_READ entry by a character's operator.

CHAR_WRITE print a character.

STRING_WRITE print a message.

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Index of Library Machines

L_ARITHMETIC1: extended integer operations: MIN, MAX, INC, DEC, EXP, SQRT, LOG

VAL_ARR_RGE read a table element
STR_ARR_RGE write a table element
COP_ARR_RGE copy a table line to another
CMP_ARR_RGE compare two table lines

BASIC_IO: vt 100 style input/output

MIN	minimum of two numbers.
MAX	maximum of two numbers.
INC	increment a number.
DEC	decrement a number.
EXP	exponential.
SQRT	integer square root by default.
LOG_BY_DEFAU	LT logarithm by default.
LOG_BY_EXCES	S logarithm by excess.

L_ARRAY1: one dimensional table with initialization loop

VAL_ARRAY	value of an element (promoted operation)
STR_ARRAY	write an element (promoted operation)
SET_ARRAY	write the same value in a portion of the table

L_ARRAY3: table with non-ordered values, maximum operations

VAL_ARRAY value of an element (promoted operation).
STR_ARRAY write an element (promoted operation).
SET_ARRAY write a same value in a table portion (promoted operation).
SWAP_ARRAY exchange two elements (promoted operation).
RIGHT_SHIFT_ARRAY shift a portion to the large index (promoted operation).

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LEFT_SHIFT_ARRAY shift a portion to the small index (promoted operation).

- SEARCH_MAX_EQL_ARRAY search for a value in a portion of the table (promoted operation).
- SEARCH_MIN_EQL_ARRAY search for a value in a portion of the table (promoted operation).

REVERSE_ARRAY invert the order of the elements in a portion of the table.

L_ARRAY5: table with ordered values, sort operation

- VAL_ARRAY value of an element (promoted operation).
- STR_ARRAY write an element (promoted operation).
- SET_ARRAY write the same value in a portion of the table (promoted operation).

SWAP_ARRAY exchange two elements (promoted operation).

RIGHT_SHIFT_ARRAY shift a portion to the large index (promoted operation).

LEFT_SHIFT_ARRAY shift a portion to the small index (promoted operation).

- SEARCH_MAX_EQL_ARRAY search for a value in a portion of the table (promoted operation).
- SEARCH_MIN_EQL_ARRAY search for a value in a portion of the table (promoted operation).
- REVERSE_ARRAY invert the order of elements in a portion of the table (promoted operation).
- SEARCH_MIN_GEQ_ARRAY search for the first element that exceeds a value (promoted operation).

ASCENDING_SORT_ARRAY sort of a table portion.

L_PFNC: partial function

- VAL_PFNC value of the function for an element in its domain
- STR_PFNC overloads the partial function with a couple
- XST_PFNC tests if an index is in the partial function domain
- RMV_PFNC removes a couple from the partial function
- SET_PFNC overloads a part of the function with a constant
- SWAP_PFNC exchanges the images for two domain indexes

RIGHT_SHIFT_PFNC right shift of a domain part

LEFT_SHIFT_PFNC left shift of a domain part

SEARCH_MAX_EQL_PFNC searches for a value in the partial function

 $\ensuremath{\texttt{SEARCH_MIN_EQL_PFNC}}$ searches for a value in the partial function

REVERSE_PFNC reverses the order of elements for a portion of the domain

INDEX OF LIBRARY MACHINES

ASCENDING_SORT_PFNC sorts in a portion of the domain

L_SEQUENCE: building a sequence

LEN_SEQ	returns the current size of the sequence.
IS_FULL_SEQ	is used to determine if the sequence is full (size = LS_maxsize).
IS_INDEX_SEC	Q is used to determine whether it is a valid index.
VAL_SEQ	value of an element in the sequence.
FIRST_SEQ	returns the first element in the sequence.
LAST_SEQ	returns the last element in the sequence.
PUSH_SEQ	add vv to the end of the sequence.
POP_SEQ	removes the last element from the sequence (its value is lost).
STR_SEQ	changes the value of an element in the sequence.
RMV_SEQ	removes an element from the middle of the sequence.
INS_AFT_SEQ	inserts vv right after index ii.
CLR_SEQ	clears the sequence.
TAIL_SEQ	removes the first element from the sequence.
KEEP_SEQ	only keeps the first elements in the sequence.
CUT_SEQ	cuts the nn first elements from the sequence.
PART_SEQ	only retains part iijj in the sequence.
REV_SEQ	reverses the order of elements in the sequence.
FIND_FIRST_S	SEQ finds vv in the sequence, from the start.
FIND_LAST_S	EQ finds vv in the sequence, from the end.

L_SET: creating a set

CARD_SET	returns the cardinal for the set.
IS_FULL_SET	identifies if the set is full (card = LSET_maxsize).
IS_INDEX_SE	T identifies if a number is a valid index.
VAL_SET	value of a element in the set.
FIND_SET	finds an element in the set.
RMV_SET	removes an element from the set.
INS_SET	inserts an element in the set.
CLR_SET	clears all elements from the set.

$L_ARRAY_1_RANGE$: array of tables of the same size with numerical indexes

VAL_ARR_RGE value of an element (promoted operation).

STR_ARR_RGE	write an element (promoted operation).
COP_ARR_RGE	copy a table to another (promoted operation).
CMP_ARR_RGE	compare two tables (promoted operation).
DUP_ARR_RGE	duplicate the same table into a series of tables.
SET_ARR_RGE	copy the same value to an index set in one of the tables.
PCOP_ARR_RGE	copy part of one of the tables to a different table to a given position.
PCMP_ARR_RGE	find the first element that is different from two parts of two tables. A Boolean element indicates if this element was found and, in this case, the index of this element is returned.

L_ARRAY_3_RANGE: range of tables of the same size, with numerical indexes, and values that are not ordered, maximum operations

VAL_ARR_RGE	value of an element (promoted operation).
STR_ARR_RGE	write an element (promoted operation).
COP_ARR_RGE	copy a table to another (promoted operation).
CMP_ARR_RGE	compare two tables (promoted operation).
DUP_ARR_RGE	duplicate the same table to an array of tables (promoted opera- tion).
SET_ARR_RGE	copy the same value to a range in one of the tables (promoted operation).
PCOP_ARR_RGE	copy part of one of the tables to a different table, in a given position (promoted operation).
PCMP_ARR_RGE	find the first different element from two parts in two tables. A Boolean element indicates whether this element was found and, in this case, the index of this element is returned (promoted opera- tion).
SWAP_RGE	swap two elements in a table.

RIGHT_SHIFT_RGE shift a table range to the large index.

LEFT_SHIFT_RGE shift a table range to the small index.

SEARCH_MAX_EQL_RGE find the last element that equals a value in a table range.

SEARCH_MIN_EQL_RGE find the first element that equals a value in a table range.

 $\label{eq:reverse} \text{REVERSE_RGE} \qquad \text{reverse the order of the elements of a table part.}$

L_ARRAY_5_RANGE: array of tables of the same size, with numerical indexes, with ordered values, sort operations

VAL_ARR_RGE	value of an element (promoted operation).
STR_ARR_RGE	write an element (promoted operation).

COP_ARR_RGE	copy a table to another (promoted operation).
CMP_ARR_RGE	compare two tables (promoted operation).
DUP_ARR_RGE	duplicate the same table in a range of tables (promoted operation).
SET_ARR_RGE	copy the same value to an index range in one of the arrays (pro- moted operation).
PCOP_ARR_RGE	copy a range from one of the tables to a different table, at a given position (promoted operation).
PCMP_ARR_RGE	find the first different element in two ranges in two tables. A Boolean element indicates that this element was found and, in this case, the index of this element is returned (promoted operation).
SWAP_RGE	swap two elements in a table (promoted operation).
RIGHT_SHIFT_RGH	E shift a table range to the large index (promoted operation).
LEFT_SHIFT_RGE	shift a table range to the small index (promoted operation).
SEARCH_MAX_EQI	L_RGE search for the last element that equals a value in a table range (promoted operation).
SEARCH_MIN_EQL	_RGE search for the first element that equals a value in a table range (promoted operation).
REVERSE_RGE	reverses the order of the elements of a part of a table (promoted operation).
SEARCH_MIN_GEQ	_ RGE search for the first element that exceeds a value in a table range.
ASCENDING_SORT	'_RGE sort a table range into ascending order.
L_SEQUENCE_RA	NGE: sequence range

LEN_SEQ_RGE	determines the length of a sequence.
IS_FULL_SEQ_RGH	E determines whether a sequence is full.
IS_INDEX_SEQ_RO	GE determines whether an integer is in a sequence range.
VAL_SEQ_RGE	gives the value of a sequence for a valid index.
FIRST_SEQ_RGE	gives the first element in a sequence.
LAST_SEQ_RGE	gives the last element in a sequence.
PUSH_SEQ_RGE	adds an element to a sequence.
POP_SEQ_RGE	removes the last element from a sequence.
STR_SEQ_RGE	changes the value of a sequence element.
RMV_SEQ_RGE	removes an element from a sequence, with a size that decreases by 1.
INS_SEQ_RGE	adds an element to a sequence, with a size that increases by 1.
CLR_SEQ_RGE	clears a sequence.
TAIL_SEQ_RGE	removes the first element from a sequence.

KEEP_SEQ_RGE	only keeps in a sequence the N first elements.
CUT_SEQ_RGE	cuts the N first elements from a sequence.
PART_SEQ_RGE	only keeps in a sequence the indexes in a range between two limits.
REV_SEQ_RGE	reverses the order of the elements in a sequence.
FIND_FIRST_SEQ_	RGE finds a value in a sequence, returns a Boolean element indicat- ing that it was found and if yes returns the smallest corresponding index.
FIND_LAST_SEQ_F	RGE finds a value in a sequence, returns a Boolean element indicat-
	ing that it was found and if yes returns the largest corresponding index.
COP_SEQ_RGE	ing that it was found and if yes returns the largest corresponding
COP_SEQ_RGE CMP_SEQ_RGE	ing that it was found and if yes returns the largest corresponding index.
•	ing that it was found and if yes returns the largest corresponding index. copies from one sequence to another.

L_ARRAY_COLLECTION: collection of arrays of the same size

array

$\label{eq:lambda} \ensuremath{\mathbf{L}}\ensuremath{\mathbf{ARRAY1}}\ensuremath{\mathbf{COLLECTION}}\xspace: \ensuremath{\mathsf{collection}}\xspace: \ensuremath{\mathsf{collection}}\$

CRE_ARR_COL	returns a Boolean element indicating that there is an array free in the collection and the index of this free array (promoted oper- ation).
DEL_ARR_COL	releases the listed array (promoted operation).
VAL_ARR_COL	read a element from on of the valid arrays (promoted operation).
STR_ARR-COL	write a element from one of the valid arrays (promoted operation).
COP_ARR_COL	copies from one of the arrays to another (promoted operation).
CMP_ARR_COL	compares two tables (promoted operation).
SET_ARR_COL	copies the same value to an index range in one of the arrays.
PCOP_ARR_COL	copies part of one of the arrays to another, to a given position.
PCMP_ARR_COL	find the first different element between the two parts of the two different arrays. A Boolean element indicates if this element was found and in this case, the index of this element is returned.

L_RELATION : complete binary relations

op_reset	The relation becomes the empty relation.
op_isFullRelation	Returns TRUE only if the cardinal of the relation equals max_nb2tupple.
op_add	Adds a couple to the relation.
op_remove	Removes a couple to the relation.
op_cardinal	Returns the relation cardinal 1
op_belongsTo	Checks if a couple is present in the relation.

¹i.e. the number of couple present in the relation.

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Description of Basic Machines

The basic machines supplied with Atelier B allow either the creation of dynamic arrays that cannot be obtained using B0, or producing models using vt100 style inputs/outputs. "dynamics arrays" are arrays which size depends on the machine parameters. Such arrays cannot be realised directly in B0, the safety design of the ADA, C and C++ translators do not allow to treat this case. For example, the following construction is not allowed:

```
\begin{array}{l} \textbf{IMPLEMENTATION} \\ mm(xx) \\ \dots \\ \textbf{CONCRETE_VARIABLES} \\ mytab \\ \textbf{INVARIANT} \\ mytab \in (0..xx) \rightarrow \text{NAT} \\ \dots \\ \textbf{END} \end{array}
```

Such an array would have to be realised using BASIC_ARRAY_VAR.

The atelier actual version is composed of three basic machines:

BASIC_ARRAY_VAR Arrays with dimension 1.

BASIC_ARRAY_RGE Arrays with dimension 2.

BASIC_IO Usual inputs/outputs management.

This chapter presents this three machines.

The basic machine BASIC_IO is intended to the model designing. It mustn't be considered as safe.

WARNING: The manual implementations of the basic machines BASIC_ARRAY_VAR and BASIC_ARRAY_RGE destined for the translators supplied with Atelier B are provided as demonstration. They are not safe, and are not appropriated in all the B use contexts.

4.1 BASIC_ARRAY_VAR: Implanting a one dimensional table

OPERATIONS

VAL_ARRAY	read a table element
STR_ARRAY	write a table element

EXAMPLE

Example of use with listed sets:

MACHINE	IMPLEMENTATION
array	array_1
SETS	REFINES
$FONTS = {Times, Serif, Courier};$	array
$FTYPE = \{fixed, unfixed\}$	IMPORTS
VARIABLES	BASIC_ARRAY_VAR(FONTS,FTYPE)
fixedsz	INVARIANT
INVARIANT	$arr_vrb = fixedsz$
$fixedsz \in FONTS \rightarrow FTYPE$	INITIALISATION
INITIALISATION	STR_ARRAY(Times, unfixed);
fixedsz:={Times \mapsto unfixed,	STR_ARRAY(Serif,fixed);
Serif \mapsto fixed, Courier \mapsto fixed}	STR_ARRAY(Courier,fixed)
END	END

arr_vrb is the name of the table encapsulated by BASIC_ARRAY_VAR

DESCRIPTION

BASIC_ARRAY_VAR modelizes one dimensional arrays. Such arrays cannot be created directly in B0 if their size dependend on the machine parameters ("dynamic arrays"). The current design of ADA or C translators does not allow handling this case. The following construction is therefore illegal:

IMPLEMENTATION mm(xx)
 VARIABLES
mytab
INVARIANT
$mytab \in (0xx) \rightarrow NAT$
 END

This kind of table should be generated using BASIC_ARRAY_VAR.

MACHINE PARAMETERS

BASIC_ARRAY_VAR (BAV_INDEX, BAV_VALUE): BAV_INDEX is the set of values used to index the table, BAV_VALUE is the set of possible values for table elements.

The B language rule relating to the possible values of the BAV_VALUE parameter ensure that: if a computer variable can contain elements of MININT..MAXINT, then it can contain those of BAV_VALUE. For example, B rules forbid assigning BAV_VALUE the value of MAXINT+1,MAXINT+2

VAL_ARRAY

STR_ARRAY

syntax STR_ARRAY(ii,vv)

preconditions ii must be a BAV_INDEX and vv must be a BAV_VALUE The value vv is stored in the array at ii index.

C++ LANGUAGE

In C++, the array is realised by an integer array. The accesses to this array are done using method that refuse the index used between 0 and the array size, guaranting an optimal memory use.

The array is dynamically reserved when launching the program. If the size indicated by the formal parameters is too big, the program stops with the following message:

Virtual memory exceede in ''new''

C LANGUAGE

The realisation in C is based on the same principles as in C++. The stop message on initial reservation failure is:

Fatal error: Malloc of X bytes failed Execution of current application is aborted

ADA LANGUAGE

The use of generic packaging guarantees an optimal memory occupation. No restrictions are made on the instanciation parameters. On initial reservation failure, an exception stops the program.

PROGRAMMING

Example of use with literal sets:

	IMPLEMENTATION
	narr_1
MACHINE	REFINES
narr	narr
VARIABLES	IMPORTS
myvar	BASIC_ARRAY_VAR(02,01)
INVARIANT	INVARIANT
myvar $\in 02 \rightarrow 01$	$\operatorname{arr}_vrb = myvar$
INITIALISATION	INITIALISATION
$myvar:=\{0 \mapsto 0, 1 \mapsto 1, 2 \mapsto 1\}$	$STR_ARRAY(0,0);$
END	$STR_ARRAY(1,1);$
	$STR_ARRAY(2,1)$
	END

Another example. Only the implementation is presented. The write of a machine refined by this implementation is an exercice for the reader:

```
IMPLEMENTATION
parr_1
REFINES
parr
IMPORTS
BASIC_ARRAY_VAR(FONTS,FTYPE)
VALUES
FONTS = 5...7;
FTYPE = 3..4
INVARIANT
arr\_vrb = fixedsz
INITIALISATION
STR\_ARRAY(5,3);
STR\_ARRAY(6,4);
STR\_ARRAY(7,5)
END
```

NOTE: The possible values of the BASIC_ARRAY_VAR parameters are given by the B language rules, (refer to section 12.2 page 574 of the BBOOK)

4.2 BASIC_ARRAY_RGE: Implementing a Two Dimensional Array

OPERATIONS

VAL_ARR_RGE	read an array element
STR_ARR_RGE	write an array element
COP_ARR_RGE	copy an array line to another
CMP_ARR_RGE	compare two array lines

EXAMPLE

Example of use, two lines and three columns array:

	IMPLEMENTATION
	bitab_1
MACHINE	REFINES
bitab	bitab
SETS	IMPORTS
$LGNS = \{ll1, ll2\}$	BASIC_ARRAY_RGE(13,0255,LGNS)
VARIABLES	INVARIANT
mytab	$\operatorname{arr}_{\operatorname{rge}} = \operatorname{mytab}$
INVARIANT	INITIALISATION
mytab \in LGNS \rightarrow (13 \rightarrow 0255)	$STR_ARR_RGE(ll1,1,7);$
INITIALISATION	$STR_ARR_RGE(ll1,2,8);$
$mytab:=\{ll1 \mapsto \{1 \mapsto 7, 2 \mapsto 8, 3 \mapsto 9\},\$	$STR_ARR_RGE(ll1,3,9);$
$ll2 \mapsto \{1 \mapsto 0, 2 \mapsto 1, 3 \mapsto 2\}\}$	$STR_ARR_RGE(ll2,1,0);$
END	$STR_ARR_RGE(ll2,2,1);$
	STR_ARR_RGE(ll2,3,2)
	END

The variable arr_rge is the name of the encapsulated array par BASIC_ARRAY_RGE

DESCRIPTION

BASIC_ARRAY_RGE models two dimensional arrays. Such arrays cannot be created directly in B0 if their size depends on the machine parameters ("dynamic array"). The safe design of the ADA, C++ or C translators do not allow to treat this case. The following construction is forbidden:

```
\begin{array}{l} \textbf{IMPLEMENTATION} \\ mm(xx) \\ \textbf{...} \\ \textbf{CONCRETE_VARIABLES} \\ mytab \\ \textbf{INVARIANT} \\ mytab \in (0..10) \rightarrow (0..xx) \times (0..xx) \\ \textbf{...} \\ \textbf{END} \end{array}
```

Such an array must be implemented using BASIC_ARRAY_RGE.

MACHINE PARAMETERS

BASIC_ARRAY_RGE(BAR_INDEX,BAR_VALUE,BAR_RANGE):

BAR_INDEX represents the column indexes.

 BAR_VALUE is the set of the possible values for the array elements,

 BAR_RANGE represents the line indexes.

The B language rules concerning the possible values of the BAR_VALUE parameter ensure that a computing variable being able to contain the elements of MININT..MAXINT, then it can contain those of BAR_VALUE. For example, the B rules do not permit to give to BAR_VALUE the value MAXINT+1,MAXINT+2.

VAL_ARR_RGE

syntax	$vv \leftarrow VAL_ARR_RGE(rr,ii)$
preconditions	ii must be a BAR_INDEX, rr must be a BAR_RANGE
outputs	vv is an element of BAR_VALUE, which value is the array value at position ii, line rr.

STR_ARR_RGE

syntax STR_ARR_RGE(rr,ii,vv)

preconditions rr must be an element of BAR_RANGE, ii an element of BAR_INDEX and vv an element of BAR_VALUE

Value vv is stored in the array line rr, index ii.

COP_ARR_RGE

syntax COP_ARR_RGE(dest,src)

preconditions dest and src must be elements of BAR_RANGE

The src line is copied to the dest line.

CMP_ARR_RGE

syntax	$bb \leftarrow CMP_ARR_RGE (range1, range2)$
preconditions	range1 and range2 must be elements of BAR_RANGE
outputs	bb is an element of BOOL, that takes the TRUE value if the two lines
	are equal.

C++ LANGUAGE

In C++, the array is realised by an array of pointers, pointing on integers arrays. The access to these arrays are done using methods that refuse the index used between 0 and the arrays size, guaranting an optimal memory occupation.

The memory is dynamically reserved when lauching the program. If the size indicated by the formal parameters is too big, the program stops with the following message:

Virtual memory exceeded in 'new'

C LANGUAGE

The realisation in C is based on the same principles as in C++. The stop message on the initial reservation failure is: Fatal error: Malloc of X bytes failed Execution of current application is aborted

ADA LANGUAGE

The use of generic packages guarantees an optimal memory occupation. No restriction is made on the instancing parameters. On an initial reservation failure, an exception stops the program.

4.3 BASIC_IO: vt100 style inputs/outputs

OPERATIONS

INTERVAL_READ operator input of an integer in mm..nn.

INT_WRITE	print an integer.	
BOOL_READ	operator input of a Boolean TRUE or FALSE state	
BOOL_WRITE	print TRUE or FALSE.	
CHAR_READ	operator input of a character.	
CHAR_WRITE	print a character.	
STRING_WRITE print a message.		

SIMPLE EXAMPLE

The following implementation displays "hello" on the terminal:

MACHINE bonj OPERATIONS main = skip END	IMPLEMENTATION bonj_1 REFINES bonj IMPORTS BASIC_IO OPERATIONS main = BEGIN STRING_WRITE("hello\n") END END

DESCRIPTION

BASIC_IO is used for simple input/output actions on a terminal. This basic machine is used to build models. Such I/O cannot be considered as safe.

In UNIX, the system devices used are standard input and standard output (*stdin* and *stdout*), they can therefore be redirected.

INTERVAL_READ

syntax	$bb \leftarrow INTERVAL_READ($	(mm,nn)
--------	---------------------------------	---------

preconditions~ mm and nn must be NATs so that mm $\leq\!$ nn

outputs bb integer in mm..nn

The operator inputs an integer of the interval mm..nn. The input format forces to type a succession of number(s) followed by RETURN. The first input character must be a number. On the opposite case, the input fails " 3" is not valid). When a character that is not the first input is not a number anymore, this character, as all the following ones, are ignored: "3e2" is a valid input of the integer 3. As long as the input is false, the message "THIS IS NOT A NUMBER IN mm..nn" is displayed and a new entry is required.

INT_WRITE

syntax	$INT_WRITE(vv)$

preconditions vv must belong to NAT

Output number vv, with no return.

BOOL_READ

syntax $bb \leftarrow BOOL_READ$ outputsbb must be Boolean.

The operator enters Boolean TRUE or FALSE conditions, with no character before it (for example: "TRUE" is rejected because of the space before it). As long as the operator has not made a valid entry, the message "THIS IS NOT A BOOL VALUE: type TRUE or FALSE" is displayed and a new entry is required.

BOOL_WRITE

syntax BOOL_WRITE(bb)

preconditions bb must be Boolean

Output TRUE or FALSE, with no return.

CHAR_READ

syntax $cc \leftarrow CHAR_READ$

outputs cc must be part of 0..255

Operator entry of a character that is interpreted as a number in 0..255. Type in the character followed by return. If several characters has been typed, only the first one is taken into account (example: "cdef" is understood as "=32). In C, pressing Return only returns 10, ctrl-D (EOF) returns 0. In ADA, only the 'visible' characters entries (i.e, no control characters) are accepted.

CHAR_WRITE

syntax CHAR_WRITE(vv)

preconditions vv must belong to the range 0..255

Displays the cc character on-screen (example: CHAR_WRITE(10) to produce a return). Remember, a single quote means "prime" the language's notation conventions, and B. CHAR_WRITE('A') for example, means nothing. On the contrary, the quoted strings are valid elements in a formula, they serve for STRING_WRITE below.

STRING_WRITE

syntax STRING_WRITE(ss)

preconditions so must be an element in the STRING set

Will display a character string on-screen. For ss use quoted strings. A "C type" formatting is used, even for a translation into ADA, i.e,:

\t produces a tab

\E produces Escape

\B produces a sound

" produces a quote

KNOWN PROBLEMS

STRING does not have a coherent definition. The prover proves that any character string belongs to STRING due to an *ad hoc* rule, that does not derive from the definition STRING = seq(CHAR). In addition, using a STRING type local variable in an implementation is not possible. To be completely rigorous, nothing ensures that the operator performs all the requested entries. Therefore the operations for entering the true data entry module (BASIC_IO.c for example) do not really implant the specifications of the corresponding B operations.

PROGRAMMING

A more complete example:

MACHINE bio OPERATIONS main = skip END	<pre>IMPLEMENTATION bio_1 REFINES bio IMPORTS BASIC_ARITHMETIC,BASIC_IO OPERATIONS main = VAR zz,bb,cc IN zz ← INTERVAL_READ(0,100); STRING_WRITE("this is the value : "); INT_WRITE(zz); CHAR_WRITE(10); bb ← BOOL_READ; STRING_WRITE("this is the value : "); BOOL_WRITE(bb); CHAR_WRITE(10); cc ← CHAR_READ; STRING_WRITE("this is the value : "); INT_WRITE(cc); STRING_WRITE(" = "); CHAR_WRITE(10) END END</pre>
--	--

Execution example:

ATELIER-B% bio sdfsdf THIS IS NOT A NUMBER IN 0..100 20 this is the value: 20 CRUE THIS IS NOT A BOOL VALUE: type TRUE or FALSE TRUE this is the value: TRUE cvf this is the value: 99 = c ATELIER-B%

NOTE: To be completely rigorous, nothing ensures that the operator performs all the entries requested. The entry loops of the concrete module (BASIC_IO.c for example) do not really implant the specifications of the corresponding operations.

Possible evolutions:

It should be possible to define in the machine BASIC_IO., abstract variables modeling the inputs/outputs; it should then be possible to specify the required interactions of the external system. The abstract machine that needs to handle inputs/outputs will use BASIC_IO notions (by SEES or INCLUDES) to represent the required interactions.

Reusable Components—Reference Manual

5 Description of Library Machines

The library machines are all intended for creating mathematical objects, except machine L_ARITHMETIC1 that provides certain arithmetical functions. The modeled mathematical objects are:

total functions : these are machines contain "ARR" (array) in their name;

partial functions : machines with the "PFNC" (partial function) in their name;

sets : these are machines with the "SET" (set) in their name;

sequences : these are machines with the "SEQ" (sequence) in their name.

For each mathematical object, it is possible to realize either a variable representing the object, or a variable representing several objects of this type. For each type of object, it is therefore possible to realize:

- The object itself;
- An array of objects with the same type, same size, these are machines with a name containing the "RGE" (range) radical;
- A partial function of objects with the same size and same type, these are machines with a name containing the "COL" (collection) radical;
- A partial function of objects with the same type, but with various sizes ("OBJ" radical).

The "RGE" and "COL" type machines produce objects that consume the memory necessary for the maximum number of required objects. For example, if we create a range or a collection of three sequences of at least ten elements, we will always require 30 memory spaces; but the use of a collection avoids the user program to manage the sequences available/occupied. Object machines reserve a memory space that may be freely distributed depending on the created objects and their size. Mathematical objects listed above are not all available on the different types of machines, refer to library machines table of contents for the list that corresponds to the current version.

WARNING : Most of the library machines are based on the basic machines BASIC-ARRAY_VAR and BASIC_ARRAY_RGE. The manual implementations of the basic machines BASIC_ARRAY_VAR and BASIC_ARRAY_RGE destined to the translators supplied with Atelier B are provided as a demonstration. They are not safe, and not appropriate in all the B use context. In the case of a more complete use, the user would have to realize these basic machines.

5.1 L_ARITHMETIC1: Extended Integer Operations

The "integer" term refers to the elements of NAT.NAT that is the set of the natural integers between 0 and MAXINT.

OPERATIONS

MIN	minimum of two integers.	
MAX	maximum of two integers.	
INC	increment an integer strictly inferior to MAXINT.	
DEC	decrement a literal integer.	
EXP	exponentiation.	
SQRT	default integer square root.	
LOG_BY_DEFAULT default logarithm.		
LOG_BY_EXCESS logarithm by excess.		

EXAMPLE

The example below shows a machine that uses a certain number of functionalities of the machine L_ARITHMETIC1.

MACHINE	IMPLEMENTATION
m1	m1_1
OPERATIONS	REFINES
$xx \leftarrow op1 = any tt where$	m1
$tt \in NAT \land tt \times tt = 16$	IMPORTS
THEN	L_ARITHMETIC1,
xx:=tt	OPERATIONS
END;	$xx \leftarrow op1 = begin$
$xx \leftarrow op2 = any tt where$	$xx \leftarrow SQRT(16)$
tt \in NAT $\land 3^{tt} = 27$	END;
THEN	$xx \leftarrow op2 = VAR rr IN$
xx:=tt	$xx, rr \leftarrow LOG_BY_DEFAULT (3, 27)$
END	END
END	END

DESCRIPTION

L_ARITHMETIC1 offers arithmetical operations such as roots and logarithms, operations on the elements NAT and dedicated to calculatory applications. Calculus being integers values, the search operation for the logarithm and the square root return the *best*¹ approaching value in NAT. The used algorithms are optimized.

MACHINE PARAMETERS

None.

 $^{^1}$ The NAT element immediatly inferior or superior we ther the calcul is performed by inferior value or superior value

MIN

syntax	$uu \leftarrow MIN(vv,ww)$
preconditions	vv and ww must be in NAT.
outputs	$uu = \min(\{vv,ww\})$

\mathbf{MAX}

syntax	$uu \leftarrow MAX(vv,ww)$
preconditions	vv and ww must be in NAT.
outputs	uu receives $\max(\{vv,ww\})$

INC

syntax	$uu \leftarrow INC(vv)$
preconditions	vv must be in 0MAXINT-1.
outputs	uu = vv+1

DEC

syntax	$uu \leftarrow DEC(vv)$
preconditions	vv must be in 1MAXINT.
outputs	uu = vv-1

\mathbf{EXP}

syntax	$\mathrm{rr} \leftarrow \mathrm{EXP}(\mathrm{xx},\mathrm{nn})$
preconditions	xx and nn must be in NAT. xx and nn must not both be nil. xx^{nn} must be less than or equal to MAXINT.
outputs	rr receives xx^{nn}

EXP returns xx to the power of nn. Calculating 0^0 is illegal (0^0 is not defined). The implementation uses a fast algorithm based on breaking down into base 2 of nn ($\log_2(nn)$ iterations).

SQRT

syntax	$nn \leftarrow SQRT(pp)$
preconditions	pp must be in NAT.
outputs	nn so that $nn \times nn \le pp < (nn+1) \times (nn+1)$

SQRT returns the largest nn so that $nn \times nn \leq pp$. The implementation uses an algorithm that performs SQRT(nn) iterations, where each iteration costs two additions and a subtraction.

LOG_BY_DEFAULT

syntax	uu,rr \leftarrow LOG_BY_DEFAULT(vv,ww)
preconditions	ww and vv are two natural integers and vv is between 2 and MAXINT.
outputs	uu is the smallest natural so that $vv^{(uu+1)}$ is strictly greater than ww.
	By definition, uu is a natural integer. rr takes the value vv^{uu} .

LOG_BY_DEFAULT in base vv of ww: returns the smallest uu value so that ww<vv^(uu+1). This gives vv^{uu} \leq ww, except if ww<vv (example: ww = 0). Does not work for vv = 0 or 1 as 0ⁱⁱ and 1ⁱⁱ are constants. rr receives the value of vv^{uu}, which easily allows judging the error made.

LOG_BY_EXCESS

syntax	uu,bb $\leftarrow \text{LOG_BY_EXCESS}(vv,ww)$
preconditions	ww belongs to NAT and vv is an element of the intervall 2MAXINT.
outputs	uu receives the smallest natural so that vv^{uu} is greater than or equal to ww. uu must be in NAT. bb is an element of BOOL, it indicates whether the logarithm is an exact one.

LOG_BY_EXCESS in base vv in ww: returns the smallest uu so that ww \leq vv^{uu}. WARN-ING: vv^{uu} may exceed MAXINT! Does not work for vv = 0 or 1 as 0ⁱⁱ and 1ⁱⁱ are constants. bb equals TRUE if ww = vv^{uu}.

IMPORTS REQUIRED

None.

5.2 L_ARRAY1: One Dimensional Array, with Initialization Loop

OPERATIONS

VAL_ARRAY	value of an element (promoted operation)
STR_ARRAY	write an element (promoted operation)
SET_ARRAY	write the same value in a portion of the array

EXAMPLE

Use SET_ARRAY to initialize an array:

MACHINE m1 VARIABLES vv INVARIANT $vv \in 010 \rightarrow 0255$ INITIALISATION $vv :=(010) \times \{5\}$ END	IMPLEMENTATION m1_1 REFINES m1 IMPORTS i1.L_ARRAY1(0255,10) INVARIANT (arr_vrb is the variable in L_ARRAY1) i1.arr_vrb = vv INITIALISATION i1.SET_ARRAY(0,10,5) END
--	--

DESCRIPTION

As it is possible, L_ARRAY1 is used instead of BASIC_ARRAY_VAR. L_ARRAY1 realises, using an array, an abstract variable representing a function. It is then possible to have an initialization operation of the entire function or of a part of it (initialization loop).

The starting part of the function performed is an interval: if not, it would not be possible to indicate a portion of this set without mentioning all elements involved.

MACHINE PARAMETERS

L_ARRAY1(LAU_VALUE, LAU_maxidx): LAU_VALUE is the set of possible values for the array elements, 0..LAU_maxidx is the set of array indexes.

VAL_ARRAY

syntax	$vv \leftarrow VAL_ARRAY(ii)$
preconditions	ii must be in 0LAU_maxidx
outputs	vv is an element of LAU_VALUE, the array value at position ii.

STR_ARRAY

syntax STR_ARRAY(ii,vv)
preconditions ii and vv must belong to the 0..LAU_maxidx and LAU_VALUE respectively.

vv value is stored in the array at ii index. **SET_ARRAY**

syntax SET_ARRAY (ii,jj,vv)

The value vv is stored in the array for all the indexes between ii to jj. If ii>jj, the array does not change.

Note that it would not have been advisable to set $ii \leq jj$ as a precondition of this operation, as this would have limited its use. Let us consider the case of a call to SET_ARRAY in a loop. The last iteration fo the loop contain s a call with the form SET_ARRAY (ii, jj, vv) with ii=jj+1. The presence of a precondition in the definition of the operation SET_ARRAY would force us to "guard" all the calls to SET_ARRAY by an IF. More generally, the precondition must be selected as minimal to protect us fromm a B code of "defensive" aspect.

IMPORTS REQUIRED

None.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_VAR machine (IMPORTS BASIC_ARRAY_VAR(...)). The addition of an instance of the machine BASIC_ARRAY_VAR requires choosing a new instance name, as, for example: i1.BASIC_ARRAY_VAR).

²Indeed, the loops used make a pre-incrementation, that does not produce literal excedent)

5.3 L_ARRAY3: Array with Non Ordered Values, Maximum Operations

OPERATIONS

VAL_ARRAY	value of an element (promoted operation).		
STR_ARRAY	write an element (promoted operation).		
SET_ARRAY	write the same value in an array portion (promoted operation).		
SWAP_ARRAY	exchange two elements (promoted operation).		
RIGHT_SHIFT_ARRAY shift a portion to the main index (promoted operation).			
LEFT_SHIFT_ARRAY shift a portion to the small index (promoted operation).			
SEARCH_MAX_EQL_ARRAY search for a value in an array (promoted operation).			
SEARCH_MIN_EQL_ARRAY search for a value in an array portion (promoted opera-			
	tion).		
DEVEDSE ADDAV	neverse the order of elements in an amoun portion		

REVERSE_ARRAY reverse the order of elements in an array portion.

EXAMPLE

The example below is a machine that represents the color assigned to 101 points, this color may be red, green or blue for each point. An operation is used to find a red dot.

$\label{eq:main_series} \begin{array}{l} \textbf{MACHINE} \\ m1 \\ \textbf{SETS} \\ \textbf{COLOR} = \{ \text{red, green, blue} \} \\ \textbf{VARIABLES} \\ \textbf{color} \\ \textbf{INVARIANT} \\ \textbf{color} \in 0100 \rightarrow \textbf{COLOR} \\ \textbf{INITIALISATION} \\ \textbf{color} := (0100) \times \{ \text{red} \} \\ \textbf{OPERATIONS} \\ \textbf{ii,bb} \leftarrow \textbf{trouve_red} = \textbf{PRE} \\ \textbf{rouge} \in \textbf{ran(color)} \\ \textbf{THEN} \\ \textbf{ii} :\in \textbf{color}^{-1}[\{ \text{red} \}] \mid \\ \textbf{bb} :\in \textbf{BOOL} \\ \textbf{END} \\ \textbf{END} \end{array}$	<pre>IMPLEMENTATION m1_1 REFINES m1 IMPORTS i1.L_ARRAY3(COLOR,100) INVARIANT i1.arr_vrb = color INITIALISATION i1.SET_ARRAY(0,100,red) OPERATIONS ii.bb ← trouve_red = VAR bb IN ii.bb ← i1.SEARCH_MAX_EQL_ARRAY(0,100,red) END END</pre>
--	---

DESCRIPTION

L_ARRAY3 is the most complete of the one dimensional array machines that do not require that the output set be part of an interval. L_ARRAY5 has been constrained. It is therefore possible to create arrays with values that are elements of a listed set while having access to complete operations such as element order reversal. The operation that

is not available is the one that would require an order relationship on the array elements: sort.

MACHINE PARAMETERS

L_ARRAY3(LAT_VALUE,LAT_maxidx): LAT_VALUE is the set of possible values for array elements, 0..LAT_maxidx is the set of array indexes.

VAL_ARRAY

syntax	$vv \leftarrow VAL_ARRAY(ii)$
preconditions	ii must be in 0LAT_maxidx
outputs	vv is a LAT_VALUE, it is the value of the array at position ii.

STR_ARRAY

syntax STR_ARRAY(ii,vv)

preconditions ii must be in 0..LAT_maxidx and vv must belong to LAT_VALUE

The vv value is stored in the array at index ii.

SET_ARRAY

syntax SET_ARRAY(ii,jj,vv)

preconditions ii..jj must be a subset of 0..LAT_maxidx and vv belong to LAT_VALUE. For implementation reasons it is also necessary that jj be different from MAXINT.

The vv value is stored in the array for all indexes between ii and jj. If ii>jj, the array will not change.

SWAP_ARRAY

syntax SWAP_ARRAY(ii,jj)

preconditions ii,jj must be in 0..LAT_maxidx.

The ii and jj elements in the array are exchanged.

RIGHT_SHIFT_ARRAY

syntax RIGHT_SHIFT_ARRAY(ii,jj,nn)

preconditions ii,jj,nn must be in 0..LAT_maxidx, with $ii \leq jj$ and $jj+nn \leq LAT_maxidx$ to make possible the possible the shift to the right by nn spaces.

Part ii+nn..jj+nn receives a copy of part ii..jj of the array (shift nn spaces to the right).

LEFT_SHIFT_ARRAY

syntax	$LEFT_{}$	SHIFT_A	ARRAY	(ii,jj,nn)	ļ
--------	-----------	---------	-------	------------	---

preconditions ii,jj must be in 0..LAT_maxidx, with $ii \leq jj$. nn must be NAT with $nn \leq ii$ to make possible the shift to the left by nn places. For implementation reasons, jj must be not equal MAXINT.

The ii-nn..jj-nn part receives a copy of part ii..jj from the array (shift nn spaces to the left).

SEARCH_MAX_EQL_ARRAY

$syntax$ rr,bb \leftarrow SEARCH_N	
preconditions ii and jj must be in 0.	.LAT_maxidx, ii $\leq jj$ and vv belong to LAT_VALUE.
outputs TRUE if vv was foun is the largest index in	d, FALSE if not rr is a NAT, if $bb = TRUE$ then rr in the array worth vv.

Search for an array element equal to vv, by scanning the ii..jj part starting from jj.

SEARCH_MIN_EQL_ARRAY

syntax	$rr,bb \leftarrow SEARCH_MIN_EQL_ARRAY(ii,jj,vv)$
preconditions	ii and jj must be in 0LAT_maxidx, ii \leq jj and vv belong to LAT_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if $bb = TRUE$, then
	rr is the smallest index in the array worth vv.

Search for an array element that equals vv, by scanning the ii..jj part starting from ii.

REVERSE_ARRAY

syntax REVERSE_ARRAY(ii,jj)

preconditions ii and jj must be in 0..LAT_maxidx.

Reverse the order of elements in the ii..jj portion of the array.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES)

BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_VAR machine (clause IMPORTS BASIC_ARRAY_VAR(...)). Therefore if another instance is necessary, it must be given a different instance name (for example: i1.BASIC_ARRAY_VAR).

5.4 L_ARRAY5: Array with Ordered Values, Sort Operation

OPERATIONS

VAL_ARRAY	value of an element (promoted operation).	
STR_ARRAY	write an element (promoted operation).	
SET_ARRAY	write the same value to a portion of an array (promoted operation).	
SWAP_ARRAY	exchange two elements (promoted operation).	
RIGHT_SHIFT_ARRAY	shift a portion to the large index (promoted operation).	
LEFT_SHIFT_ARRAY	shift a portion to the small index (promoted operation).	
SEARCH_MAX_EQL_ARRAY search for a value in a portion of the array (promoted operation).		
SEARCH_MIN_EQL_ARRAY search for a value in a portion of the array (promoted operation).		
REVERSE_ARRAY	reverse the order of the elements in a portion of the array (promoted operation).	
SEARCH_MIN_GEQ_ARRAY search for the first element that exceeds a value (pro- moted operation).		
ACCENERIC CODE ADE		

ASCENDING_SORT_ARRAY sort a portion of the array.

EXAMPLE

	IMPLEMENTATION
MACHINE	m1_1
m1	REFINES
VARIABLES	m1
VV	IMPORTS
INVARIANT	$L_{ARRAY5(0,255,4)}$
$vv \in 04 \rightarrow 0255 \wedge$	INVARIANT
$\forall xx.(xx \in 03 \Rightarrow$	$\operatorname{arr_vrb} = vv$
$vv(xx) \ge vv(xx+1))$	INITIALISATION
INITIALISATION	$SET_ARRAY(0,4,50);$
vv : (vv $\in 04 \rightarrow 0255 \land$	$STR_ARRAY(2,10);$
$\forall xx.(xx \in 03 \Rightarrow$	$STR_ARRAY(4,30);$
$vv(xx) \ge vv(xx+1)))$	ASCENDING_SORT_ARRAY(0,4);
END	REVERSE_ARRAY(0,4)
	END

DESCRIPTION

L_ARRAY5 is the most complete of the one dimensional array machines. It especially comprises a sort operation implanted using a shift sort (fast algorithm).

MACHINE PARAMETERS

L_ARRAY5(LAC_minval,LAC_maxval,LAC_maxidx): LAC_minval..LAC_maxval is the set of possible values for the elements in the array, 0..LAC_maxidx is the set of index values for the array. LAC_minval, LAC_maxval, LAC_maxidx must be NATs: this machine does not allow negative values. It is also necessary for LAC_minval \leq LAC_maxval and $1\leq$ LAC_maxidx.

VAL_ARRAY

syntax	$vv \leftarrow VAL_ARRAY(ii)$
preconditions	ii must be in 0LAC_maxidx
outputs	vv is in LAC_minvalLAC_maxval, is the array value at position ii.

STR_ARRAY

syntax STR_ARRAY(ii,vv) preconditions ii must be in 0..LAC_maxidx and vv in LAC_minval..LAC_maxval and LAC_VALUE.

The vv value is stored in the array at index ii.

SET_ARRAY

syntax SET_ARRAY(ii,jj,vv)

preconditions ii..jj must be included in 0..LAC_maxidx and vv must be in LAC_VALUE. For implementation, it is also necessary that jj be different from the MAXINT constant.

The vv value is stored in the array for all indexes from ii to jj. If ii>jj, the array does not change.

SWAP_ARRAY

syntax SWAP_ARRAY(ii,jj)

preconditions ii,jj must be in 0..LAC_maxidx.

The ii and jj elements in the array are exchanged.

RIGHT_SHIFT_ARRAY

syntax RIGHT_SHIFT_ARRAY(ii,jj,nn)

preconditions ii,jj,nn must be in 0..LAC_maxidx, with ii≤jj and jj+nn≤LAC_maxidx to make possible the right shift by nn spaces.

The ii+nn..jj+nn part receives a copy of the ii..jj part of the array (shift right by nn spaces).

LEFT_SHIFT_ARRAY

syntax LEFT_SHIFT_ARRAY(ii,jj,nn)

 $\begin{array}{ll} preconditions & \mbox{ii,jj must be in 0..LAC_maxidx, with ii \leq jj. nn must be a NAT with nn \leq \mbox{ii} \\ & \mbox{to allow the left shift by nn spaces. For implementation reasons, jj cannot equal MAXINT.} \end{array}$

The ii-nn.jj-nn part receives a copy of the ii.jj part of the array (shift left by nn spaces).

SEARCH_MAX_EQL_ARRAY

syntax	$rr,bb \leftarrow SEARCH_MAX_EQL_ARRAY(ii,jj,vv)$
preconditions	ii and jj must be in 0LAC_maxidx, ii \leq jj and vv be in LAC_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if $bb = TRUE$, then
	rr is the highest index in the array worth vv.

Search for an array element equal to vv, by scanning the ii..jj part starting from jj.

SEARCH_MIN_EQL_ARRAY

syntax	$rr,bb \leftarrow SEARCH_MIN_EQL_ARRAY(ii,jj,vv)$
preconditions	ii and jj must be in 0LAC_maxidx, ii \leq jj and vv be in LAC_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if $bb = TRUE$ then
	rr is the smallest index in the array worth vv.

Search for an array element equal to vv, by scanning the ii..jj part starting from ii.

REVERSE_ARRAY

syntax REVERSE_ARRAY(ii,jj)

preconditions ii and jj must be in 0..LAC_maxidx.

Reverse the order of the elements in the ii..jj portion of the array.

SEARCH_MIN_GEQ_ARRAY

syntax	$ii,bb \leftarrow SEARCH_MIN_GEQ_ARRAY(jj,kk,vv)$
preconditions	jj and kk must be in 0LAC_maxidx, jj \leq kk and vv be in LAC_minval LAC_maxval. For implementation location reasons, kk must not equal the MAXINT constant.
outputs	TRUE if an element that is greater or equal to vv was found, FALSE if not. ii is a NAT, if bb = TRUE, then ii is the smallest index in the image array that is greater than or equal to vv.

Search for an element that is greater than or equal to vv in jj..kk starting from jj.

ASCENDING_SORT_ARRAY

syntax ASCENDING_SORT_ARRAY(ii,jj)

preconditions ii and jj must be in 0..LAC_maxidx. For implementation reasons, ii and jj must not equal MAXINT.

Shift sort, in ascending order (the smallest first) on the ii..jj portion.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine sees them with SEES)

BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_VAR machine (clause IMPORTS BASIC_ARRAY_VAR(...)). Therefore if another instance is required it must be given a different instance name (for example: i1.BASIC_ARRAY_VAR).

5.5 L_PFNC: Partial Function

OPERATIONS

VAL_PFNC	value of the function for an element in its domain	
STR_PFNC	overloads the partial function with a pair	
XST_PFNC	test that an index is in the partial function domain	
RMV_PFNC	removes a pair from the partial function	
SET_PFNC	overloads a part of the function with a constant	
SWAP_PFNC	exchanges the images for two domain indexes	
RIGHT_SHIFT_PFNC right shift part of the domain		
LEFT_SHIFT_PFNC left shift part of the domain		
SEARCH_MAX_EQL_PFNC search for a value in the partial function		
SEARCH_MIN_EQL_PFNC search for a value in the partial function		
REVERSE_PFNC reverse the order of elements in a portion of the domain		
ASCENDING_SORT_PFNC sort in a portion of the domain		

EXAMPLE

	IMPLEMENTATION
MACHINE	m1_1
m1	REFINES
VARIABLES	m1
pf	IMPORTS
INVARIANT	$L_{PFNC}(0,255,10)$
$pf \in 010 \rightarrow 0255$	INVARIANT
INITIALISATION	$pfnc_vrb = pf$
$\mathrm{pf} := \{4 \mapsto 6\}$	INITIALISATION
END	$STR_PFNC(4,6)$
	END

DESCRIPTION

L_PFNC implements a partial function with almost all of the operations available in L_ARRAY5 (In fact only SEARCH_MIN_GEQ is not used). The practical usefulness of partial functions is that they dispense with the need to add a "non existent" or "unused" element in the input sets in order to implant them as total functions. The implementation of L_PFNC performs these elements by using the seldom used MAXINT value.

MACHINE PARAMETERS

L_PFNC(LPF_minval,LPF_maxval,LPF_maxidx): LPF_minval..LPF_maxval is the input set of the function, 0..LPF_maxidx is the source set. LPF_minval, LPF_maxval, LPF_maxidx must be NATs: this machine does not allow negative values. Moreover, LPF_minval \leq LPF_maxval and 1 \leq LPF_maxidx; as well as LPF_maxval<MAXINT: This is because MAXINT is used to indicate that the corresponding index is not part of the partial function. Again to simplify implementation, it is also illegal to have LPF_maxidx = MAXINT.

VAL_PFNC

syntax	$vv \leftarrow VAL_PFNC(ii)$
preconditions	ii must be in the partial function domain
outputs	vv is in LPF_minvalLPF_maxval, it is the value of the array at position ii.

STR_PFNC

syntax STR_PFNC(ii,vv)

preconditions ii must be in 0..LPF_maxidx and vv be in LPF_minval..LPF_maxval. The partial function is overloaded by $\{ii \mapsto vv\}$.

XST_PFNC

syntax	$bb \leftarrow XST_PFNC(ii)$
outputs	bb is TRUE if ii is in the domain of the function, FALSE if not.

RMV_PFNC

syntax RMV_PFNC(ii)

preconditions ii must be in the domain of the partial function.

The {ii→pfnc_vrb(ii)} pair is removed from the partial function pfnc_vrb.

SET_PFNC

syntax	SET_PFNC(ii,jj,vv)
preconditions	iijj must be included in 0LPF_maxidx and vv be in LPF_minvalLPF-
	_maxval. ii and jj must be NATs.

The partial function is overloaded by (ii..jj)×vv. If ii>jj,

ii..jj is blank and the partial function is not modified, but it is still necessary for ii and jj to be NATs.

SWAP_PFNC

syntax SWAP_PFNC(ii,jj)

preconditions ii, jj must be in the domain of the partial function.

The ii and jj elements in the array are exchanged.

RIGHT_SHIFT_PFNC

syntax RIGHT_SHIFT_PFNC(ii,jj,nn)

preconditions ii,jj,nn must be in 0..LPF_maxidx, with ii ≤ jj and jj+nn ≤ LPF_maxidx to allow the right shift by nn spaces. It is also necessary for ii..jj to be included in the domain of the partial function.

The ii+nn.jj+nn part is overloaded by a copy of the ii.jj part in the partial function (shift by nn spaces to the right).

LEFT_SHIFT_PFNC

syntax LEFT_SHIFT_PFNC(ii,jj,nn)

preconditions ii, jj must be in 0..LPF_maxidx, with $ii \leq jj$. nn must be a NAT with $nn \leq ii$ to allow the left shift by nn spaces. In addition it is necessary for ii..jj to be included in the domain of the partial function.

The ii-nn.jj-nn part is overloaded by a copy of the ii.jj part in the partial function (shift left by nn spaces).

SEARCH_MAX_EQL_PFNC

syntax	$rr,bb \leftarrow SEARCH_MAX_EQL_PFNC(ii,jj,vv)$
preconditions	ii and jj must be in 0 LPF_maxidx, ii $\leq jj$ and vv be in LPF_minval LPF_maxval.
outputs	TRUE if vv was found, FALSE if not, rr is a NAT, if $bb = TRUE$, then rr is the largest index, the image of which by the partial function is vv.

Search for an array element that equals vv, by scanning the ii..jj part, starting from jj.

SEARCH_MIN_EQL_PFNC

syntax	$rr,bb \leftarrow SEARCH_MIN_EQL_PFNC(ii,jj,vv)$
preconditions	ii and jj must be in 0 LPF_maxidx, ii $\leq jj$ and vv be in LPF_minval LPF_maxval.
outputs	TRUE if vv was found, FALSE if not, rr is a NAT, if $bb = TRUE$, then rr is the smallest index, the image of which by the partial function is vv.

Search for an array element that equals vv, by scanning the ii..jj part starting from ii.

REVERSE_PFNC

syntax REVERSE_PFNC(ii,jj)

preconditions ii and jj must be in 0..LPF_maxidx, and ii..jj must be included in the domain of the partial function.

Reverse the order of the elements in the ii..jj portion of the partial function.

ASCENDING_SORT_PFNC

syntax ASCENDING_SORT_PFNC(ii,jj)

preconditions ii and jj must be in 0..LPF_maxidx, and ii..jj must be included in the domain of the partial function.

Shift sort, in ascending order (the smallest first) in the ii..jj portion.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES) BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_VAR machine (clause IMPORTS BASIC_ARRAY_VAR(...)). Therefore if another instance is necessary, it must be given a different instance name (for example: i1.BASIC_ARRAY_VAR).

5.6 L_SEQUENCE: Creating a Sequence

OPERATIONS

LEN_SEQ	returns the current size of the sequence.			
IS_FULL_SEQ	IS_FULL_SEQ shows whether the sequence is full (size = $LS_{maxsize}$).			
IS_INDEX_SE	Q shows whether ii is a valid index.			
VAL_SEQ	value of an element in the sequence.			
FIRST_SEQ	returns the first element in the sequence.			
LAST_SEQ	returns the last element in the sequence.			
PUSH_SEQ	adds vv to the end of the sequence.			
POP_SEQ	removes the last element from the sequence (its value is lost).			
STR_SEQ	changes the value of an element in the sequence.			
RMV_SEQ	removes an element from the middle of the sequence.			
INS_AFT_SEQ inserts vv right after index ii.				
CLR_SEQ	clears the sequence.			
$TAIL_SEQ$	removes the first element from the sequence.			
KEEP_SEQ	only keeps the nn first elements in the sequence.			
CUT_SEQ	cuts the nn first elements from the sequence.			
PART_SEQ	only keeps the iijj portion in the sequence.			
REV_SEQ	reverses the order of the elements in the sequence.			
FIND_FIRST_SEQ searches for vv in the sequence, starting from the beginning.				
FIND_LAST_SEQ searches for vv in the sequence, starting from the end.				

EXAMPLE

The example below shows the use of L_SEQUENCE for a listed set.

$\label{eq:main_second} \begin{array}{l} \textbf{MACHINE} \\ m1 \\ \textbf{SETS} \\ ST = \{classic, baroque\} \\ \textbf{VARIABLES} \\ vv \\ \textbf{INVARIANT} \\ vv \in seq(ST) \land \\ size(vv) \leq 10 \\ \textbf{INITIALISATION} \\ vv := [baroque, baroque] \end{array}$	IMPLEMENTATION m1_1 REFINES m1 IMPORTS L_SEQUENCE(10,ST) INVARIANT (seq_vrb is the variable in L_SEQUENCE) seq_vrb = vv INITIALISATION PUSH_SEQ(baroque) (L_SEQUENCE guarantees PUSH_SEQ(baroque) that the sequence is empty at the start) END
---	---

DESCRIPTION

L_SEQUENCE provides a sequence type variable, the maximum size of which is a machine parameter. Conventional search and shift functions are provided for the practical use of this sequence. This answers the frequent problem in programming applications which is to maintain a list with no blanks.

MACHINE PARAMETERS

L_SEQUENCE(LS_maxsize,LS_VALUE): the variable is a sequence of LS_VALUE elements, with a maximum size that is LS_maxsize.

LEN_SEQ

syntax nn \leftarrow LEN_SEQ

outputs 0..LS_maxsize

Returns the current size of the sequence.

IS_FULL_SEQ

syntax	$bb \leftarrow IS_FULL_SEQ$	
outputs	bb is TRUE if the sequence is full, FALSE if not.	
Specifies whether the sequence is full (size = $LS_maxsize$).		

IS_INDEX_SEQ

syntax	$bb \leftarrow IS_INDEX_SEQ(ii)$
preconditions	ii must be a NAT.

outputs bb is TRUE if ii is an index in the sequence, FALSE if not. Specifies whether ii is a valid index.

VAL_SEQ

	syntax	$vv \leftarrow VAL_SEQ(ii)$
	preconditions	ii must be an index in the sequence (ii \in 1size(seq_vrb)).
	outputs	vv is the value of the ii-ith element (vv \in VALUE).
Value of an element in the sequence.		

FIRST_SEQ

syntax	$vv \leftarrow FIRST_SEQ$	
preconditions	the sequence must not be empty.	
outputs	vv is the value of the first element (vv \in VALUE).	
Returns the first element in the sequence.		

LAST_SEQ

syntax	$vv \leftarrow LAST_SEQ$	
preconditions	the sequence must not be empty.	
outputs	vv is the value of the last element (vv \in VALUE).	
Returns the last element in the sequence.		

PUSH_SEQ

syntax PUSH_SEQ(vv)

preconditions vv must be in VALUE and the sequence must not be full. Add vv at the end of the sequence.

POP_SEQ

syntax POP_SEQ

preconditions the sequence must not be empty.

Removes the last element from the sequence (its value is lost).

STR_SEQ

syntax STR_SEQ(ii,vv)

preconditions vv must be in VALUE and ii must be a valid index for the sequence. Changes the value of an existing element in the sequence.

RMV_SEQ

syntax RMV_SEQ(ii)

preconditions ii must be a valid index in the sequence.

Removes an element from the middle of the sequence.

INS_AFT_SEQ

syntax INS_AFT_SEQ(ii,vv)

preconditions vv must be in VALUE and ii must be a valid index for the sequence. The sequence must not be full.

Inserts vv right after index ii.

CLR_SEQ

syntax CLR_SEQ Clears the sequence.

TAIL_SEQ

syntax TAIL_SEQ

preconditions the sequence must not be empty.

Removes the first element from the sequence.

KEEP_SEQ

syntax KEEP_SEQ(nn)

preconditions nn must be a NAT.

Only retains the nn first elements in the sequence. For $nn = size(seq_vrb)$, this operation does not take action.

CUT_SEQ

syntax CUT_SEQ(nn)

preconditions nn must be a NAT.

Deletes the nn first elements from the sequence. For $nn = size(seq_vrb)$, this operation is equivalent to CLR_SEQ.

PART_SEQ

syntax PART_SEQ(ii,jj)

preconditions ii and jj must be non null NATs, with $ii \leq jj$.

Only retains the ii..jj portion in the sequence. ii..jj may not be included in the domain of the sequence.

REV_SEQ

syntax REV_SEQ

Reverses the order of the elements in the sequence. Applies even for sequences that are empty or of size 1.

FIND_FIRST_SEQ

syntax	bb,ii $\leftarrow \text{FIND_FIRST_SEQ(vv)}$
preconditions	vv must be in VALUE.
outputs	bb is TRUE if vv is in the sequence, FALSE if not. ii belongs to the range $1LS_maxsize$, if $bb = TRUE$, then it indicates the first position equal to vv.

Search for vv in the sequence, starting from the start.

FIND_LAST_SEQ

syntax	bb,ii \leftarrow	$FIND_LAST_SEQ(vv)$
0,9.00000	~~,	

preconditions vv must be in VALUE.

outputs bb is TRUE if vv is in the sequence, FALSE if not. If bb = TRUE, ii belongs to the range 1..LS_maxsize and indicates the last position equal to vv.

Search for vv in the sequence, starting from the end.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES) BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_VAR machine (clause IMPORTS BASIC_ARRAY_VAR(...)). Therefore if another instance is required, it must be given a non blank instance name (for example: i1.BASIC_ARRAY_VAR).

5.7 L_SET: Creating a Set

OPERATIONS

CARD_SET	returns the cardinal for the set.	
IS_FULL_SET	identifies whether the set is full (card = LSET_maxsize).	
FIND_SET	finds an element in the set.	
RMV_SET	removes an element from the set.	
INS_SET	inserts an element in the set.	
CLR_SET	removes all of the elements from the set.	
IS_INDEX_SET identifies whether a number is a valid index.		
VAL_SET	value of an element in the set.	

EXAMPLE

The example below shows the use of L_SET on a listed set.

$\label{eq:matrix} \begin{array}{l} \textbf{MACHINE} \\ m1 \\ \textbf{SETS} \\ ST = \{ \text{cat, dog, bird} \} \\ \textbf{VARIABLES} \\ vv \\ \textbf{INVARIABLES} \\ vv \subseteq ST \\ \textbf{INVARIANT} \\ vv \subseteq ST \\ \textbf{INITIALISATION} \\ vv := \{ \text{cat, bird} \} \\ \textbf{END} \end{array}$	IMPLEMENTATION m1_1 REFINES m1 IMPORTS L_SET(3,ST) INVARIANT (set_vrb is the variable in L_SET) ran (set_vrb) = vv INITIALISATION (L_SET ensures that the set is empty at the start) INS_SET(cat); INS_SET(bird) END
---	---

DESCRIPTION

L_SET creates a set that is modeled by an injective sequence type variable, set_vrb the maximum size of which is a machine parameter. It offers functions to search for, add and delete elements.

The use of an injective sequence type variable enables easy access to each element of the set via an index. The user can therefore create loops by using the CARD_SET and VAL_SET functions. This would not have been possible if the variable directly represented the set.

WARNING: The user must add the gluing invariant $ran(set_vrb) = var_locale$ to his machine in order to link his set variable with the L_SET machine state.

MACHINE PARAMETERS

L_SET (LSET_maxsize, LSET_VALUE): the variable is an injective sequence of elements from LSET_VALUE, with a maximum size LSET_maxsize.

CARD_SET

syntax	$nn \leftarrow CARD_SET$
output	nn is the size of the set (the cardinal of ran (set_vrb)). Therefore, nn belongs to 0 LSET_maxsize

Returns the size of the set.

IS_FULL_SET

syntax	$bb \leftarrow IS_FULL_SET$	
output	bb is TRUE if the set is full, FALSE if not.	
States whether the set is full (size = $LSET_maxsize$).		

IS_INDEX_SET

syntax	$bb \leftarrow IS_INDEX_SET(ii)$	
preconditions	ii must be a NAT.	
outputs	bb is TRUE if ii is an index of the set, FALSE if not.	
States whether ii is a valid index.		

VAL_SET

syntax	$vv \leftarrow VAL_SET(ii)$	
preconditions	ii must be an index of the set (ii $\in 1size(seq_vrb)$).	
outputs	vv is the value of the ii-the element (vv \in LSET_VALUE).	
Value of an element of the set.		

FIND_SET

syntax	bb, ii \leftarrow FIND_SET(vv)
preconditions	vv must be in LSET_VALUE.
outputs	bb is TRUE if vv is in the set, FALSE if not. ii is a NAT, if $bb = TRUE$, then it indicates the position of element vv.

Search for vv in the set.

$\mathbf{RMV_SET}$

syntax RMV_SET(vv)

 $preconditions\;$ vv must be in the set.

Removes an element from the set.

INS_SET

syntax INS_SET(vv)

preconditions vv must be in LSET_VALUE.

Adds an element to the end of the set, if it is not already in it, if not it does nothing.

CLR_SET

syntax CLR_SET

Clears the set.

5.8 L_ARRAY1_ RANGE: A Range of Arrays of the Same Size, with Numerical Indexes

OPERATIONS

VAL_ARR_RGE	value of an element (promoted operation).	
STR_ARR_RGE	write an element (promoted operation).	
COP_ARR_RGE	copy an array to another (promoted operation).	
CMP_ARR_RGE	compare two arrays (promoted operation).	
DUP_ARR_RGE	duplicate the same array to a series of arrays.	
SET_ARR_RGE	copy the same value to an index interval in one of the arrays.	
PCOP_ARR_RGE	copy part of one array to a different array, to a given position.	
PCMP_ARR_RGE	search for the first element that is different between two parts of two arrays. A Boolean element indicates whether this element was found and, in this case, the index of this element in returned.	

EXAMPLE

Using SET_ARR_RGE and DUP_ARR_RGE to initialize a set of arrays:

$\begin{tabular}{lllllllllllllllllllllllllllllllllll$	IMPLEMENTATION m1_1 REFINES m1 IMPORTS i1.L_ARRAY1_RANGE(0,20,10,0255) INVARIANT i1.arr_rge = vv INITIALISATION i1.SET_ARR_RGE(0,0,10,5); i1.DUP_ARR_RGE (1,20,0) END
---	--

DESCRIPTION

L_ARRAY1_RANGE is used in place of BASIC_ARRAY_RANGE, so that a range of arrays may create a set of function type abstract variables when operations are required to perform complete array initialization.

It also allows performing operations that use parts of two different arrays.

The index and range sets are intervals so that it is possible to indicate only portions of these sets without listing all elements involved.

MACHINE PARAMETERS

L_ARRAY1_RANGE (LAUR_minrge, LAUR_maxrge, LAUR_maxidx, LAUR_VALUE): The range interval is the LAUR_minrge..LAUR_maxrge interval, the index interval is 0..LAUR_maxidx and LAUR_VALUE is the set of possible values.

VAL_ARR_RGE

syntax	$vv \leftarrow VAL_ARR_RGE (range, index)$
preconditions	range must belong to LAUR_minrgeLAUR_maxrge and index belong to 0LAUR_maxidx.
outputs	vv is a LAUR_VALUE, it is the value of the array range at the index position.

STR_ARR_RGE

syntax	STR_ARR_RGE (range, index, value)		
preconditions	range must belong to LAUR_minrgeLAUR_maxrge, index belong to		
	0LAUR_maxidx and value belong to LAUR_VALUE.		

The value data value is stored in the indexed array range.

COP_ARR_RGE

syntax	COP_ARR_RGE	(dest, src)
--------	-------------	-------------

preconditions dest and src are in LAUR_minrge..LAUR_maxrge

The src array is copied to the dest array.

CMP_ARR_RGE

syntax	$bb \leftarrow CMP_ARR_RGE (range1, range2)$
preconditions	range1 and range2 are in LAUR_minrgeLAUR_maxrge
outputs	bb is a BOOL element that is TRUE if the two arrays are equal and FALSE if not.

SET_ARR_RGE

syntax

SET_ARR_RGE (range,ii,jj,vv)

preconditions range must belong to LAUR_minrge..LAUR_maxrge, ii..jj be included in 0..LAUR_maxidx and vv belong to LAUR_VALUE. For implementation reasons, jj must also be different from MAXINT.

The vv value is stored in the array range for all index values between ii and jj. If ii>jj, the array remains unchanged.

DUP_ARR_RGE

syntax	DUP_ARR_RGE	(dest1, dest2, src)
giveau		(access, access)

preconditions dest1, dest2, src are in LAUR_minrge..LAUR_maxrge. For implementation reasons, dest2 must also be different from MAXINT.

The src array is duplicated in all of the arrays of the dest1..dest2 interval.

PCOP_ARR_RGE

syntax PCOP_ARR_RGE (dest, idx_dst, src,ii,jj)

preconditions dest and src must be different elements of LAUR_minrge..LAUR_maxrge, ii..jj be a non empty interval of 0..LAUR_maxidx, idx_dst belong to 0..LAUR_maxidx, jj be different from MAXINT and idx_dst + jj - ii belong to 0..LAUR_maxidx (condition necessary to ensure that the copy does not overflow).

The ii..jj part of the src array is copied to the dest array, from the idx_dst index.

PCMP_ARR_RGE

syntax $idx, bb \leftarrow PCMP_ARR_RGE (rng2,idx2,rng1)$	tax id	$idx, bb \leftarrow$	PCMP_ARR_RGE	(rng2,idx2,rng1,ii,jj)
---	--------	----------------------	--------------	------------------------

preconditions rng1 and rng2 must belong to LAUR_minrge..LAUR_maxrge, ii..jj be a non empty interval of 0..LAUR_maxidx, idx2 and idx2 + jj-ii are in 0..LAUR_maxidx.

The ii..jj part of array rng1 is compared to the part with the same size in the rng2 array. The idx2 + jj-ii $\in 0..LAUR_maxidx$ condition guarantees that this comparison is possible. bb is a Boolean element that is FALSE if the two parts are equal and TRUE if they are different. In the latter case, idx and index are the first element that is different from ii..jj.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES) $BASIC_ARITHMETIC$, $BASIC_BOOL$.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_RANGE machine (IMPORTS BASIC_ARRAY_RANGE(...) clause). Therefore if another instance is necessary, it must be given the name of a non empty instance (for example: i1.BASIC_ARRAY_RANGE).

5.9 L_ARRAY3_RANGE: A Range of Arrays of the Same Size, with Non Ordered Values, Maximum Operations

OPERATIONS

VAL_ARR_RGE	value of an element (promoted operation).
STR_ARR_RGE	write an element (promoted operation).
COP_ARR_RGE	copy an array to another (promoted operation).
CMP_ARR_RGE	compare two arrays (promoted operation).
DUP_ARR_RGE	duplicate the same array to a set of arrays (promoted operation).
SET_ARR_RGE	copy the same value to an index interval in one of the arrays (promoted operation).
PCOP_ARR_RGE	copy part of one of the arrays to a different array, at a given position (promoted operation).
PCMP_ARR_RGE	search for the first element that is different between two parts of two arrays. A Boolean element indicates whether this element was found and, in this case, the index of this element is returned (promoted operation).
SWAP_RGE	exchange two array elements.
RIGHT_SHIFT_RGI	E shift part of an array to the large index.
LEFT_SHIFT_RGE	shift part of an array to the small index.
SEARCH_MAX_EQ	L_RGE search for the last element that equals a value in part of an array.
SEARCH_MIN_EQL	_RGE search for the first element that equals a value in part of an array.
REVERSE_RGE	reverse the order of the elements in part of an array.

EXAMPLE

The following example is a machine that represents the color assigned to 101 dots for each array in a range; this color may be red, green or blue for each dot. A operation enables finding a red dot in an array.

MACHINE	
m3	IMPLEMENTATION
SETS	m3_1
$COLOR = \{red, green, blue\}$	REFINES
VARIABLES	m3
color	IMPORTS
INVARIANT	i1.L_ARRAY3_RANGE(0,10,100,COLOR)
$color \in 010 \rightarrow (0100 \rightarrow COLOR)$	INVARIANT
INITIALISATION	$i1.arr_rge = color$
$color:=(010) \times \{(0100) \times \{red\}\}$	INITIALISATION
OPERATIONS	$il.SET_ARR_RGE(0,0,100,red);$
ii,bb \leftarrow find_red(rng) = PRE	$il.DUP_ARR_RGE(1,10,0)$
$\mathrm{rng} \in 010$ \wedge	OPERATIONS
$rouge \in ran(color(rng))$	$ii,bb \leftarrow find_red(rng) = VAR bb IN$
THEN	ii,bb ←
$ii:\in color(rng)^{-1}[\{red\}] \parallel$	i1.SEARCH_MAX_EQL_RGE(rng,0,100,red)
bb:∈ BOOL	END
END	END
END	

DESCRIPTION

L_ARRAY3_RANGE is the most complete of the two dimensional array machines with no constraint³. This makes it possible to create arrays with values that are the elements of an enumerated set, while retaining access to complete operations such are reversing the order of elements.

The operation that is not available is the one that would require an order relation on the elements in the array: sort.

MACHINE PARAMETERS

L_ARRAY3_RANGE (LATR_minrge, LATR_maxrge, LATR_maxidx, LATR_VALUE):

The range interval is LATR_minrge..LATR_maxrge, the index interval 0..LATR_maxidx and LATR_VALUE is the set of possible values.

VAL_ARR_RGE

syntax	$vv \leftarrow VAL_ARR_RGE (range, index)$
preconditions	range must belong to LATR_minrge LATR_maxrge, index belong to $0{\rm LATR}_{\rm maxidx}$
outputs	vv is a LATR_VALUE, it is the value of the array range at the index position.

STR_ARR_RGE

syntax STR_ARR_RGE (range, index, value)

preconditions range must belong to LATR_minrge..LATR_maxrge, index belong to 0..LATR_maxidx and value belong to LATR_VALUE.

The LATR_VALUE value is stored in the array range in the index.

³L_ARRAY5_RANGE can only have a finite integer set as range.

COP_ARR_RGE

syntax	COP_ARR_RGE	(dest. src)
syntua		(ucst, sic)

preconditions dest and src are in LATR_minrge..LATR_maxrge

The src array is copied to the dest array.

CMP_ARR_RGE

syntax	$bb \leftarrow CMP_ARR_RGE (range1, range2)$
preconditions	range1 and range2 are in LATR_minrgeLATR_maxrge
outputs	bb is an BOOL that equals TRUE if the two arrays are equal and FALSE
	if not.

SET_ARR_RGE

syntax SET_ARR_RGE (range,ii,jj,vv)
 preconditions range must belong to LATR_minrge..LATR_maxrge, ii..jj be included in 0..LATR_maxidx and vv belong to LATR_VALUE. For implementation reasons, jj must also be different to MAXINT.

Value vv is stored in the array range for all indexes in the range from ii to jj. If ii>jj, the array remains unchanged.

DUP_ARR_RGE

syntax	$DUP_ARR_RGE (dest1, dest2, src)$
preconditions	dest1, dest2, src are in LATR_minrgeLATR_maxrge. For implementa-
	tion reasons, dest2 must also be different to MAXINT.

The src array is duplicated in all of the arrays of the dest1..dest2 interval.

PCOP_ARR_RGE

syntax PCOP_ARR_RGE (dest, idx_dst, src,ii,jj)

preconditions dest and src must belong to LATR_minrge..LATR_maxrge and be different, ii..jj be a non empty interval of 0..LATR_maxidx, idx_dst belong to 0..LATR_maxidx, jj be different from MAXINT and idx_dst + jj - ii belong to 0..LATR_maxidx (necessary condition to avoid copy overflow).

The ii..jj part in the src array is copied to the dest array, from the idx_dst index.

PCMP_ARR_RGE

syntax	idx, bb $\leftarrow \text{PCMP_ARR_RGE} (rng2,idx2,rng1,ii,jj)$
preconditions	rng1 and rng2 are in LATR_minrgeLATR_maxrge, iijj is a non empty interval of 0LATR_maxidx idx2 and idx2 + jj-ii are in 0LATR_maxidx.
	11100 1000

The ii..jj part of array rng1 is compared with the part with the same size in array rng2. The idx2 + jj-ii \in 0..LATR_maxidx condition guarantees that this comparison is possible. bb is a Boolean element that is FALSE if the two parts are equal and TRUE if they are different. In the latter case, idx is the index of the first element that is different to ii..jj.

SWAP_RGE

syntax SWAP_RGE (rng,ii,jj)

preconditions rng is in LATR_minrge..LATR_maxrge, ii and jj in 0..LATR_maxidx. The ii and jj elements in the array are exchanged.

RIGHT_SHIFT_RGE

syntax RIGHT_SHIFT_RGE (rng,ii,jj,nn)

preconditions rng must belong to LATR_minrge..LATR_maxrge, ii, jj and nn belong to $0..LATR_maxidx$, with $ii \leq jj$ and $jj+nn \leq LATR_maxidx$ to allow a right shift by nn spaces.

The ii+nn.jj+nn part in the rng array receives a copy of the ii.jj part of this same array (shift right by nn spaces).

LEFT_SHIFT_RGE

syntax LEFT_SHIFT_RGE (rng,ii,jj,nn)

 $\begin{array}{ll} preconditions & {\rm rng\ is\ in\ LATR_minrge..LATR_maxrge;\ ii,jj\ must\ be\ in\ 0..LATR_maxidx,} \\ & {\rm with\ ii\leq jj.\ nn\ must\ be\ a\ NAT\ with\ nn\ \leq\ ii\ to\ allow\ the\ left\ shift\ by\ nn} \\ & {\rm spaces.\ For\ implementation\ reasons,\ jj\ must\ be\ equal\ to\ MAXINT.} \end{array}$

The ii-nn..jj-nn part of the rng array receives a copy of the ii..jj part of this same array (shift left by nn spaces).

SEARCH_MAX_EQL_RGE

syntax	$rr,bb \leftarrow SEARCH_MAX_EQL_RGE (rng,ii,jj,vv)$
preconditions	rng must be in LATR_minrgeLATR_maxrge. ii and jj must be in 0LATR_maxidx, ii \leq jj and vv must belong to LATR_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if $bb = TRUE$ then rr is the largest index in the rng array equal to vv.

Search for an element in an array equal to vv, by scanning the ii.jj part starting from jj.

SEARCH_MIN_EQL_RGE

syntax	$rr,bb \leftarrow SEARCH_MIN_EQL_RGE (rng,ii,jj,vv)$
preconditions	rng must belong to LATR_minrgeLATR_maxrge, ii and jj belong to 0LATR_maxidx, ii \leq jj and vv belong to LATR_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if bb = TRUE, then rr is the smallest index in the rng array equal to vv.

Search for an element in an array that is equal to vv, by scanning the ii..jj part starting from ii.

REVERSE_RGE

syntax REVERSE_RGE(rng,ii,jj)

preconditions rng must belong to LATR_minrge..LATR_maxrge, ii and jj belong to 0..LATR_maxidx.

Reversing the order of elements in the ii..jj part of the rng array.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES) BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_RANGE machine (IMPORTS BASIC_ARRAY_RANGE(...) clause). Therefore if another instance is necessary, it must be given a non empty instance name (for example: i1.BASIC_ARRAY_RANGE)

5.10 L_ARRAY5_RANGE: Range of Arrays of the Same Size, with Ordered Value Numerical Indexes, Sort Operation

OPERATIONS

VAL_ARR_RGE	value of an element (promoted operation).	
STR_ARR_RGE	write an element (promoted operation).	
COP_ARR_RGE	copy an array to another (promoted operation).	
CMP_ARR_RGE	compare two arrays (promoted operation).	
DUP_ARR_RGE	duplicate the same array to a set of arrays (promoted operation).	
SET_ARR_RGE	copy the same value to an index range in one of the arrayx (pro- moted operation).	
PCOP_ARR_RGE	copy part of one of the arrays to a different array, to a given position (promoted operation).	
PCMP_ARR_RGE	search for the first different element between two parts of two ar- rays. A Boolean element indicates whether this element was found and, in this case, the index of this element is returned (promoted operation).	
SWAP_RGE	exchange two elements in an array (promoted operation).	
RIGHT_SHIFT_RG	E shift a part of an array to the large index (promoted operation).	
LEFT_SHIFT_RGE	shift a part of an array to the small index (promoted operation).	
SEARCH_MAX_EQL_RGE search for the last element that is equal to a value in an array range (promoted operation).		
SEARCH_MIN_EQL	RGE search for the fist element that equals a value in an array range (promoted operation).	
REVERSE_RGE	reverse the order of the elements of a part of an array (promoted operation).	
SEARCH_MIN_GEG	Q_ RGE search for the first element that exceeds a value in an array range.	
ASCENDING_SORT	LRGE sort part of an array and arrange in ascending order.	

EXAMPLE

	$\label{eq:mbound} \begin{array}{l} \textbf{IMPLEMENTATION} \\ m5_1 \\ \textbf{REFINES} \\ m5 \\ \textbf{IMPORTS} \\ \textbf{L}_ARRAY5_RANGE(0,20,4,0,255) \\ \textbf{INVARIANT} \\ arr_rge = vv \\ \textbf{INITIALISATION} \\ SET_ARR_RGE(0,0,4,50); \\ STR_ARR_RGE(0,2,10); \\ STR_ARR_RGE(0,2,10); \\ STR_ARR_RGE(0,4,30); \\ ASCENDING_SORT_RGE(0,0,4); \\ REVERSE_RGE(0,0,4); \\ DUP_ARR_RGE(1,20,0) \\ \textbf{END} \end{array}$
--	---

DESCRIPTION

L_ARRAY5_RANGE is the most complete two dimensional array machines. It especially contains a sort operation, implanted by a shift sort (fast algorithm).

MACHINE PARAMETERS

L_ARRAY5_RANGE (LACR_minrge, LACR_maxrge, LACR_maxidx, LACR_minval, LACR_maxval):

LACR_minrge.LACR_maxrge is the set of ranges, 0..LACR_maxidx is the set of indexes and LACR_minval.LACR_maxval, the set of possible values. All of the parameters must be NATs: this machine does not allow negative values.

In addition, LACR_minrge \leq LACR_maxrge, 1 \leq LACR_maxidx and LACR_minval \leq LACR_maxval.

VAL_ARR_RGE

syntax	$vv \leftarrow VAL_ARR_RGE (range, index)$
preconditions	range must belong to LACR_minrgeLACR_maxrge, index belong to 0LACR_maxidx.
outputs	vv is a LACR_VALUE, it is the value of the array range at the index position.

STR_ARR_RGE

syntax STR_ARR_RGE (range, index, value)

preconditions range must be in LACR_minrge..LACR_maxrge index must be in 0 .. LACR_maxidx value must belong to LACR_VALUE.

The value of the value element is stored in the array range as an index.

COP_ARR_RGE

syntax COP_ARR_RGE (dest, src)

preconditions dest and src are in LACR_minrge..LACR_maxrge

The src array is copied to the dest array.

CMP_ARR_RGE

syntax	$bb \leftarrow CMP_ARR_RGE (range1, range2)$
preconditions	range1 and range2 are in LACR_minrgeLACR_maxrge
outputs	bb is a BOOL element that is TRUE if the two arrays are equal and FALSE if not.

SET_ARR_RGE

syntax SET_ARR_RGE (range,ii,jj,vv)
 preconditions range must belong to LACR_minrge..LACR_maxrge, ii..jj be included in 0..LACR_maxidx and vv belong to LACR_VALUE. For implementation reasons, it is also necessary that jj be different from MAXINT.

The vv value is stored in the array range for all indexes between ii and jj. If ii>jj, the array remains unchanged.

DUP_ARR_RGE

syntax DUP_ARR_RGE (dest1, dest2, src)

preconditions dest1, dest2, src are in LACR_minrge..LACR_maxrge. For implementation reasons, it is also necessary for dest2 to be different from MAXINT.

The src array is duplicated to all arrays for the dest1..dest2 range.

PCOP_ARR_RGE

syntaxPCOP_ARR_RGE (dest, idx_dst, src,ii,jj)preconditionsdest and src must be different elements of LACR_minrge..LACR_maxrge,
ii..jj be a non empty subset of 0..LACR_maxidx and idx_dst belong to

0..LACR_maxidx; jj is different from MAXINT and idx_dst + jj - ii belong to 0..LACR_maxidx (condition to avoid copy overflow).

The ii..jj range in the src array is copied to the dest array, for the idx_dst index.

PCMP_ARR_RGE

syntax idx, bb \leftarrow PCMP_ARR_RGE (rng2,idx2,rng1,ii,jj)

preconditions rng1 and rng2 are in LACR_minrge..LACR_maxrge, ii..jj is a non empty range 0..LACR_maxidx, idx2 and idx2 + jj-ii are in 0..LACR_maxidx.

The ii..jj part of the rng1 array is compared with the part of the same size in the rng2 array. The idx2 + jj-ii \in 0..LACR_maxidx condition guarantees that this comparison is possible. bb is a Boolean element that is FALSE if the two parts are equal and TRUE if they are different. In the latter case, idx is the index of the first element that is different from ii..jj.

SWAP_RGE

syntax SWAP_RGE (rng,ii,jj)

preconditions rng is in LACR_minrge..LACR_maxrge, ii and jj in 0..LACR_maxidx. The ii and jj elements in the array are exchanged.

RIGHT_SHIFT_RGE

syntax RIGHT_SHIFT_RGE (rng,ii,jj,nn)

preconditions rng must belong to LACR_minrge..LACR_maxrge. ii, jj and nn belong to 0..LACR_maxidx, with ii ≤ jj and jj+nn ≤ LACR_maxidx to allow the shift right by nn spaces.

The ii+nn.jj+nn part of the rng array receives a copy of the ii..jj part from this same array (shift nn spaces to the right).

LEFT_SHIFT_RGE

syntax LEFT_SHIFT_RGE (rng,ii,jj,nn)

preconditions rng must belong to LACR_minrge..LACR_maxrge, ii and jj belong to $0..LACR_maxidx$, with $ii \leq jj$. nn must belong to NAT with nn $\leq ii$ to make possible the left shift by nn spaces. For implementation reasons, jj cannot equal MAXINT.

The ii-nn.jj-nn part of the rng array receives a copy of the ii.jj part of this same array (shift nn spaces to the left).

SEARCH_MAX_EQL_RGE

syntax	$rr,bb \leftarrow SEARCH_MAX_EQL_RGE (rng,ii,jj,vv)$
preconditions	rng must belong to LACR_minrgeLACR_maxrge. ii and jj belong to $0LACR_maxidx$, ii $\leq jj$ and vv must belong to LACR_VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if $bb = TRUE$ then rr the largest index in the array that equals vv.

Search for an array element that equals vv, by scanning the ii..jj part starting from jj.

SEARCH_MIN_EQL_RGE

syntax	$rr,bb \leftarrow SEARCH_MIN_EQL_RGE (rng,ii,jj,vv)$
preconditions	rng must belong to LACR_minrgeLACR_maxrge, ii and jj belong to 0LACR_maxidx, ii \leq jj and vv must belong to VALUE.
outputs	TRUE if vv was found, FALSE if not. rr is a NAT, if bb = TRUE, then rr is the smallest index in the rng array equal to vv.

Search for an element in an array equal to vv, by scanning the ii..jj part starting from ii.

REVERSE_RGE

syntax REVERSE_RGE(rng,ii,jj)

preconditions rng must belong to LACR_minrge..LACR_maxrge, ii and jj belong to 0..LACR_maxidx.

Reverse the order of elements in the ii.jj range of the rng array.

SEARCH_MIN_GEQ_RGE

syntax	$ii,bb \leftarrow SEARCH_MIN_GEQ_RGE(rng,jj,kk,vv)$
preconditions	rng must belong to LACR_minrgeLACR_maxrge. jj and kk belong to $0LACR_maxidx, jj \le kk$ and vv belong to LACR_minvalLACR_maxval. For implementation reasons, kk must be different from MAXINT.
outputs	bb is a Boolean element, TRUE is an element that exceeds or is equal to the vv value found, FALSE if not. ii is a NAT, if bb = TRUE, then ii is the smallest index in the image array that exceeds or is equal to vv.

Search for an element that exceeds or is equal to vv in the jj..kk range, starting from jj.

ASCENDING_SORT_RGE

syntax ASCENDING_SORT_RGE (rng,ii,jj)

preconditions rng must belong to LACR_minrge..LACR_maxrge, ii and jj belong to 0..LACR_maxidx. For implementation reasons, ii and jj must not be different from MAXINT.

Shift sort, in ascending order (starting with the smallest) on the ii..jj range in an array.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES)

BASIC_ARITHMETIC; BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_RANGE machine (IMPORTS BASIC_ARRAY_RANGE(...) clause). Therefore if another instance is necessary, it must be given a non empty instance name (for example: i1.BASIC_ARRAY_RANGE)

5.11 L_SEQUENCE_RANGE: Range of Sequences

OPERATIONS

LEN_SEQ_RGE	gives the size of a sequence.	
IS_FULL_SEQ_RGE	indicates whether a sequence is full.	
IS_INDEX_SEQ_RG	E indicates whether an integer is in the sequence domain.	
VAL_SEQ_RGE	gives the value of a sequence for a valid index.	
FIRST_SEQ_RGE	gives the first element of a sequence.	
LAST_SEQ_RGE	gives the last element of a sequence.	
PUSH_SEQ_RGE	adds an element to a sequence.	
POP_SEQ_RGE	removes the last element from a sequence.	
STR_SEQ_RGE	changes the value of an element in a sequence.	
RMV_SEQ_RGE	removes an element from a sequence, the size of which is reduced by 1.	
INS_SEQ_RGE	adds an element to a sequence, the size of which increases by 1.	
CLR_SEQ_RGE	empties a sequence.	
TAIL_SEQ_RGE	removes the first element from a sequence.	
KEEP_SEQ_RGE	only retains the first N in a sequence elements.	
CUT_SEQ_RGE	cuts the N first elements from a sequence.	
PART_SEQ_RGE	only retains in a sequence the indexes between the two limit values.	
REV_SEQ_RGE	reverses the order of the elements in a sequence.	
FIND_FIRST_SEQ_RGE searches for a value in a sequence, returns a Boolean element indicating whether it was found, and if yes, returns the smallest corresponding index.		
FIND_LAST_SEQ_F	RGE searches for a value in a sequence, returns a Boolean element indicating whether it was found and if yes, returns the largest corresponding index.	
COP_SEQ_RGE	copies one of the sequences to another.	
CMP_SEQ_RGE	compares two sequences.	
DCOD SEO DCE	partial conviction one accurace to another	

- PCOP_SEQ_RGE partial copy from one sequence to another.
- $\label{eq:pcmp_seq_res} \ensuremath{\mathsf{PCMP_SEQ_RGE}}\xspace \ensuremath{\mathsf{pcmp}}\xspace \ensuremath{\mathsf{pcmp}}\xsp$

EXAMPLE

The example below shows the use of L_SEQUENCE_RANGE on a numbered set.

DESCRIPTION

L_SEQUENCE_RANGE enables implementing and using a set number of sequences with a fixed maximum size. The sequence number evolves in a range that is a machine parameter, the maximum size of all of the sequences is also a machine parameter. The purpose is to be able to make comparisons and copies between these sequences directly, using an additional operation to the traditional operations on each of the sequences.

MACHINE PARAMETERS

L_SEQUENCE_RANGE (LSR_minrge, LSR_maxrge, LSR_maxsize, LSR_VALUE): the variable is a total function of LSR_minrge..LSR_maxrge in the set of VALUE sequences with a maximum size of LSR_maxisize.

LEN_SEQ_RGE

syntax	$nn \leftarrow LEN_SEQ_RGE (range)$
preconditions	range must belong to the LSR_minrgeLSR_maxrge range.
outputs	nn is the size of the range position , nn \in 0LSR_maxsize.
Gives the size of a sequence.	

IS_FULL_SEQ_RGE

	syntax	$bb \leftarrow IS_FULL_SEQ_RGE (range)$
	preconditions	range must belong to the range LSR_minrgeLSR_maxrge.
	outputs	bb is TRUE if the range position sequence is full, FALSE if not.
Indicates whether a sequence is full.		

IS_INDEX_SEQ_RGE

syntax	$bb \leftarrow IS_INDEX_SEQ_RGE (range, ii)$
preconditions	range must belong to the LSR_minrgeLSR_maxrge range, ii must be a NAT.
outputs	bb is TRUE if it is an index in the range position sequence. FALSE if not

outputs bb is TRUE if ii is an index in the range position sequence, FALSE if not. Identifies whether an integer is in a sequence domain.

VAL_SEQ_RGE

syntax	$vv \leftarrow VAL_SEQ_RGE (range, ii)$
preconditions	range must belong to the LSR_minrgeLSR_maxrge range, ii must be an index in the range position sequence (ii \in 1size (seq_rge (range))).
outputs	vv is the value of the ii-th element in the range position sequence (vv \in VALUE).

Gives the value of a sequence for a valid index.

FIRST_SEQ_RGE

syntax	$vv \leftarrow FIRST_SEQ_RGE (range)$
preconditions	range must belong to the LSR_minrgeLSR_maxrge range, the range position sequence must not be empty.
outputs	vv is the value of the first element in the range position sequence (vv \in VALUE).

Gives the first element in a sequence.

LAST_SEQ_RGE

syntax	$vv \leftarrow LAST_SEQ_RGE (range)$
preconditions	range must be in the LSR_minrgeLSR_maxrge range, the range position
	sequence must not be empty.
outputs	vv is the value of the last element in the range position sequence (vv \in VALUE).

Gives the last element of a sequence.

PUSH_SEQ_RGE

syntaxPUSH_SEQ_RGE (range, vv)preconditionsrange must belong to the LSR_minrge..LSR_maxrge range, vv must be
in LSR_VALUE and the range position sequence cannot be full.

Adds an element to a sequence.

POP_SEQ_RGE

syntax POP_SEQ_RGE (range)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, the range position sequence must not be empty.

Removes the last element in a sequence.

STR_SEQ_RGE

syntax STR_SEQ_RGE (range, ii, vv)

preconditions range must belong to LSR_minrge..LSR_maxrge, ii be a valid index in the range position sequence and vv belong to LSR_VALUE.

Change the value of an element in a sequence.

RMV_SEQ_RGE

syntax RMV_SEQ_RGE (range, ii)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, ii must be a valid index in the range sequence.

Removes an element from a sequence, the size of which decreases by 1.

INS_AFT_SEQ_RGE

syntax INS_AFT_SEQ_RGE (range, ii, vv)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, ii must be a valid index in the range position sequence, vv must be in LSR_VALUE, the range position sequence must not be full.

Adds an element to a sequence, the size of which increases by 1.

CLR_SEQ_RANGE

syntax CLR_SEQ_RANGE (range)

preconditions range must belong to the LSR_minrge..LSR_maxrge range.

Clears a sequence.

TAIL_SEQ_RGE

syntax TAIL_SEQ_RGE (range)

preconditions range must belong to the LSR_minrge..LSR_maxrge range and the range position sequence cannot be empty.

Removes the first element in a sequence.

KEEP_SEQ_RGE

syntax KEEP_SEQ_RGE (range, nn)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, nn must be a NAT.

Only retains the nn first elements in a sequence. For nn = size (seq_rge(range)); this operation has no effect.

CUT_SEQ_RGE

syntax CUT_SEQ_RGE (range, nn)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, nn must be in NAT.

Clears the sequence of its first nn elements. For $nn = size(seq_rge(range))$, this operation is equivalent to CLR_SEQ_RGE.

PART_SEQ_RGE

syntax PART_SEQ_RGE (range, ii, jj)

preconditions range must belong to the LSR_minrge..LSR_maxrge range, ii and jj must be NATs that are not null, with ii \leq jj.

In a sequence, only retains the indexes between two limits. ii..jj may not be in the sequence domain.

REV_SEQ_RGE

syntax REV_SEQ_RGE (range)

preconditions range must belong to the LSR_minrge..LSR_maxrge range.

Reverses the order of the elements in a sequence.

FIND_FIRST_SEQ_RGE

syntax	bb, ii \leftarrow FIND_FIRST_SEQ_RGE (range, vv)
preconditions	range must belong t the LSR_minrgeLSR_maxrge range, vv must be in LSR_VALUE.
outputs	bb is TRUE if vv is in the range position sequence, FALSE if not. ii is a NAT, if $bb = TRUE$, it indicates the first position that equals vv in the sequence.

Searches for a value in a sequence starting from the beginning.

FIND_LAST_SEQ_RGE

syntax	bb, ii \leftarrow FIND_LAST_SEQ_RGE (range, vv)
preconditions	range must belong to the LSR_minrgeLSR_maxrge range, vv must be in LSR_VALUE.
outputs	bb is TRUE if vv is in the range position sequence, FALSE if not. ii is a NAT; if $bb = TRUE$, this indicates the last position that equals vv in the sequence.

Searches for a value in a sequence, starting from the end.

COP_SEQ_RGE

syntax COP_SEQ_RGE (dst, src)

preconditions dst and src must belong to the LSR_minrge..LSR_maxrge range.

Copy the seq_rge(src) sequence to the seq_rge(dst) sequence.

CMP_SEQ_RGE

syntax	$bb \leftarrow CMP_SEQ_RGE (rng1, rng2)$
preconditions	rng1 and rng2 must belong to the LSR_minrgeLSR_maxrge range.
outputs	bb is TRUE if the two rng1 and rng2 position sequences are equal, FALSE if not.

Compare two sequences.

PCOP_SEQ_RGE

syntax PCOP_SEQ_RGE (dst, idx, src, ii, jj)

preconditions dst and src must belong to the LSR_minrge..LSR_maxrge range, dst must be different from src, ii and jj must be valid indexes in the src position sequence, with ii \leq jj and jj \leq MAXINT-1 idx must be a valid index for the dst sequence or where the size of this sequence +1, idx + jj - ii belongs to the 1..LSR_maxsize range.

Copy the ii..jj part of the src position sequence to the dst position from the idx index.

PCMP_SEQ_RGE

syntax	$idx, bb \leftarrow PCMP_SEQ_RGE (rng1, ii, jj, rng2, kk)$
preconditions	rng1 and rng2 must be in the LSR_minrgeLSR_maxrge range, ii and jj must be valid indexes in the rng1 and ii \leq jj position sequences, kk must be a valid index in the rng2 position sequence, (kk + jj - ii) must be a valid index in the rng2 position sequence.
output	bb is TRUE if there is an element of the iijj part in the seq_rge (rng1) sequence that is different to the kk (kk + jj - ii) part of the seq_rge (rng2) sequence, FALSE if not. idx is a NAT if bb is TRUE, the idx represents the index of the first element that is different in the seq_rge (rng1 \in iijj) sequence.

Partial comparison of two sequences.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine

sees them with SEES)

BASIC_ARITHMETIC;

BASIC_BOOL.

WARNING: The implementation of this machine creates the default instance for the BASIC_ARRAY_RANGE and BASIC_ARRAY_VAR machines. Therefore, if other instances are required they must be given a name that is not blank.

(example: i1.BASIC_ARRAY_RANGE).

5.12 L_ARRAY_COLLECTION: collection of arrays of the same size

OPERATIONS

CRE_ARR_COL	returns a Boolean element that indicates that there remains an array available in the collection and gives the index of this available array.
DEL_ARR_COL	releases the specified array.
VAL_ARR_COL	read an element from one of the valid arrays.
STR_ARR-COL	write an element from one of the valid arrays.
COP_ARR_COL	copy one of the arrays to another.
CMP_ARR_COL	compare two arrays.

EXAMPLE

	IMPLEMENTATION
	M1_1
	REFINES
MACHINE	M1
m1	IMPORTS
OPERATIONS	L_ARRAY_COLLECTION(4,110,110)
$ii1,ii2 \leftarrow initialise_arrayx(vv) = PRE$	OPERATIONS
$vv \in 110$	$ii1,ii2 \leftarrow initialise_arrayx(vv) = BEGIN$
THEN	VAR b1,b2 in
ii1:∈ NAT	ii1,b1 \leftarrow CRE_ARR_COL;
ii2:∈ NAT	$ii2,b2 \leftarrow CRE_ARR_COL;$
END	STR_ARR_COL(ii1,1,vv);
END	COP_ARR_COL(ii2,ii1)
	END
	END
	END

DESCRIPTION

L_ARRAY_COLLECTION is used to handle identically sized one dimensional arrays. It contains basic operations (create, delete, read, write, compare).

MACHINE PARAMETERS

L_ARRAY_COLLECTION (LACOLL_maxobj, LACOLL_INDEX, LACOLL_VALUE): LACOLL_maxobj is the maximum number of arrays in the collection. LACOLL_INDEX is the set of array indexes, LACOLL_VALUE is the set of possible values of array elements.

CRE_ARR_COL

Syntaxii, $bb \leftarrow CRE_ARR_COL$ Outputsbb is a Boolean element indicating whether any available arrays are left
in the collection, ii is the index of this available array.

Assigning an array in the collection.

DER_ARR_COL

Syntax DEL_ARR_COL (ii)

Preconditions ii must belong to 1..LACOLL_maxobj

The array of index ii in the collection is released. It may once again be assigned using CRE_ARR_COL.

VAL_ARR_COL

Syntax $vv \leftarrow VAL_ARR_COL$ (ii, jj)

Preconditions ii must belong to 1..LACOLL_maxobj and jj belong to LACOLL_INDEX.

Output vv contains the jj number value of array ii.

Use vv to store the value of number jj in array ii.

STR_ARR_COL

Syntax STF	_ARR_COL	(ii, j	$\mathbf{j},\mathbf{vv})$
------------	----------	--------	---------------------------

Preconditions ii must belong to 1..LACOLL_maxobj, jj belong to LACOLL_INDEX and vv belong to LACOLL_VALUE.

Write the value of vv to cell number jj in array ii.

COP_ARR_COL

Syntax COP_ARR_COL (dest, src)

Preconditions dest and src must belong to 1..LACOLL_maxobj.

Copy the contents of the src array to the dest array.

CMP_ARR_COL

Syntax bb \leftarrow CMP_ARR_COL (range 1, range 2)

Preconditions range 1 and range 2 must belong to 1..LACOLL_maxobj.

Output bb is a Boolean element indicating whether array range 1 and range 2 are identical.

Comparison between the two 2 arrays.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine sees them with SEES).

BASIC_ARITHMETIC BASIC_BOOL

5.13 L_ARRAY1_COLLECTION: array of the same size, with numerical indexes

OPERATIONS

CRE_ARR_COL	returns a Boolean element indicating whether an array remains available in the collection and the index of this available array (promoted operation).
DEL_ARR_COL	releases the array mentioned (promoted operation).
VAL_ARR_COL	read an element from one of the valid arrays (promoted operation).
STR_ARR-COL	write an element from one of the valid arrays (promoted opera- tion).
COP_ARR_COL	copy one of the arrays to another (promoted operation).
CMP_ARR_COL	compare two arrays (promoted operation).
SET_ARR-COL	copy the same value to an index range in one of the arrays.
PCOP_ARR_COL	copy part of one of the arrays to another in a given position.
PCMP_ARR_COL	search for the first different element between two parts of two different arrays. A Boolean element indicates whether the element was found and in this case, the index of this element is returned.

EXAMPLE

Using SET_ARR_COL to fill-in two arrays and PCOP_ARR_COL to define a third one. Note the need to test the Boolean output elements from CRE_ARR_COL in order to use the arrays created.

The example is as follows:

 $\begin{aligned} \mathbf{MACHINE} \\ \mathbf{M1} \\ \mathbf{OPERATIONS} \\ \mathbf{op} = \mathbf{skip} \\ \mathbf{END} \end{aligned}$

```
IMPLEMENTATION
 M1 1
REFINES
 M1
IMPORTS
 L_ARRAY1_COLLECTION(3,3,1,10)
OPERATIONS
 op = Var i1,i2,i3,b1,b2,b3 in
    i1,b1 \leftarrow CRE_ARR_COL;
    i2,b2 \leftarrow CRE\_ARR\_COL;
    i3.b3 \leftarrow CRE\_ARR\_COL;
    IF b1 = TRUE \land
      b2 = TRUE \land
      b3 = TRUE
    THEN
      SET\_ARR\_COL(i1,0,3,1);
      SET\_ARR\_COL(i2,0,3,2);
      PCOP_ARR_COL(i3,0,i1,0,1);
      PCOP_ARR_COL(i3,2,i2,2,3)
    END
 END
END
```

DESCRIPTION

L_ARRAY1_COLLECTION enables the use of a collection of arrays without the need to code loops to position a set of elements or arrays. This was not possible with the previous machine L_ARRAY_COLLECTION where index sets are normally unordered.

MACHINE PARAMETERS

L_ARRAY1_COLLECTION (LAUC_maxobj, LAUC_maxidx, LAUC_minval,

LAUC_maxval): The variable is a partial function of 1..LAUC_maxobj in the set of total functions of 0..LAUC_maxidx to LAUC_minval..LAUC_maxval. LAUC_maxobj is a NAT1 that is different from MAXINT. LAUC_maxidx, LAUC_minval and LAUC_maxval are NATs and LAUC_minval \leq LAUC_maxval.

CRE_ARR_COL

Syntaxii, bb \leftarrow CRE_ARR_COLOutputsbb is a Boolean element indicating whether any available arrays remain
in the collection, ii is the index of this available array.

Allocate an array in the collection.

DEL_ARR_COL

Syntax DEL_ARR_COL (ii)

Preconditions ii must belong to 1..LAUC_maxobj

Array ii in the collection is released. It may once again be assigned using CRE_ARR_COL.

VAL_ARR_COL

Syntax $vv \leftarrow VAL_ARR_COL (ii, jj)$

Preconditions ii must belong to 1..LAUC_maxobj jj must belong to 1..LAUC_maxidx.

Output vv contains the value of number jj in array ii.

Store in vv the value of number jj in array ii.

STR_ARR_COL

Syntax	STR_ARR_COL (ii, jj, vv)
Sgroouw	

Preconditions ii must belong to 1..LAUC_maxobj; jj must belong to 1..LAUC_maxidx. vv must belong to LAUC_VALUE.

Write value vv to the jjth cell in array ii.

COP_ARR_COL

Syntax COP_ARR_COL (dest, src)

Preconditions dest and src must belong to 1..LAUC_maxobj.

Copy the contents of the src array to the dest array.

CMP_ARR_COL

Syntax	$bb \leftarrow$	CMP_	ARR	COL	(range 1.	range 2)

Preconditions range 1 and range 2 must belong to 1..LAUC_maxobj.

Output bb is a Boolean element that indicates whether array ranges 1 and 2 are identical.

Comparison between the two arrays.

SET_ARR_COL

Syntax SET_ARR_COL (range, ii, jj, vv)

Preconditions range belonging to dom(arr_col), i.e. it corresponds to the index of a previously created array. ii and jj are in 1..LAUC_maxidx, jj must be different from MAXINT. vv is in LAUC_minval..LAUC_maxval.

The value vv is copied to the range array for all indexes between ii and jj. If ii > jj, the array remains unchanged.

PCOP_ARR_COL

Syntax PCOP_ARR_COL (dest, idx_dst, src, ii, jj)

Preconditions dest and src are elements that are different from 1..LAUC_maxobj, corresponding to arrays already created. ii..jj is a non blank interval of 0..LAUC_maxidx and jj /= MAXINT. idx_dst..idx_dst + jj - ii is an interval of 0..LAUC_maxidx.

The ii..jj part in the src array is copied to the idx_dst..idx_dst + jj - ii part of the dst array.

$PCMP_ARR_COL$

Syntax	idx, bb \leftarrow PCMP_ARR_COL (nn2, idx2, nn1, ii, jj)
Preconditions	nn1 and nn2 are elements that are different from 1LAUC_maxobj and
	correspond to arrays already created. iijj is a non blank interval of
	0LAUC_maxidx. idx2idx2 + jj - ii is an interval of 0LAUC_maxidx.
Outputs	bb is a BOOL. idx is in iijj.

The ii..jj part in array nn1 is compared to part idx2..idx2 + jj - ii in array nn2. bb is FALSE if the two parts are identical, TRUE if not. In this case, idx is the index of the first element that is different from ii..jj.

IMPORTS REQUIRED

(instances to import as the implementation tree for this library machine sees them with SEES) BASIC_ARITHMETIC, BASIC_BOOL.